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A
SUPPLEMENT
TO THE
MISCELLANEOUS
WORKS
Of the Late
Dr. ARBUTHNOT.



G L A S G O W:

Printed for JAMES CARLILE, and Sold by
the Booksellers of *Great Britain* and *Ire-
land* 1751.

TO THE
PUBLICK.

SI N C E the Publication of
the Two Volumes of this
Author's Works, some Gentlemen
have been so gracious to assist us
with the Pieces mark'd with an
Asterism, which in Justice to the
Publick we present them with
gratis.



A

SUPPLEMENT, &c.

The Freeholder's Political Catechism.

Anno 1733.

Question, **W**HO are you ?
Answer, I am T. M. a Freeholder of Great Britain.
Q. What Privileges enjoy'st thou by being a Freeholder of Great Britain ?

A. By being a Freeholder of Great Britain, I am a greater Man in my Civil Capacity, than the greatest Subject of an Arbitrary Prince ; because I am govern'd by Laws, to which I give my Consent, and my Life, Liberty, and Goods, cannot be taken from me, but according to those Laws : I am a Freeman.

Q. Who gave thee this Liberty ?
A. No Man gave it me : Liberty is the Natural Right of every Human Creature ; he is born to the Exercise of it as soon as he has attained to that of his Reason ; but that my Liberty is preserved to me, when lost to a great part of Mankind, is owing under God to the Wisdom and Valour of my Ancestors, Freeholders of this Realm.

A 2

Q. Does

VOR 20 JUN 34

Q. Does not every Man give up his Liberty, to the Government of the Political Society, whereof he is a Member ?

A. Mankind give up some part of their Natural Liberty to the Government for the Benefit of Society and mutual Defence (for in Political Society an Infant has the whole Force of the Community to protect him) but no Man can make himself a Slave.

Q. Why ?

A. Because no Man can give an absolute Dominion over his Life, for that is not in his Power and belongs only to his Creator.

Q. How comes it then that the Civil Magistrate has a Right to take away Lives ?

A. Because by the Laws of Nature, every Man has a Power of taking away the Life of another in Self-defence, which Power is given up to the Magistrate, and which Power returns to every Man, when the Magistrate cannot defend him, as in the Case of being attack'd with sudden and lawless Violence.

Q. Has not the Magistrate a Power to compel thee to be of what Religion he thinks fit.

A. No, Because neither in the State of Nature, nor in the State of Civil Society, has any Man an absolute Power over another Man's Mind or Conscience ; from whence it follows, that in the first of those States, no Man could give the Magistrate a Power which he hath not to give : and that in the Second of those States, the Exercise of this Power is impossible ; Compulsion without Conviction making a Man an Hypocrite, that is a Criminal, but can never secure the publick Peace.

Q. Wherein does this Liberty which thou enjoyest consist ?

A. In Laws made by the Consent of the People, and

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and the due Execution of those Laws; I am free
not from the Law, but by the Law.

*Q. Wilt thou stand fast in this Liberty whereunto
thou art born and entitled by the Laws of thy
Country?*

*A. Yes verily, by God's Grace I will; and I
thank his good Providence that I am born a
Member of a Community governed by Laws and
not by Arbitrary Power.*

*Q. What dost thou think incumbent upon thee to
secure this Blessing to thyself and Posterity?*

*A. As I am a Freeholder, I think it incumbent
upon me, to believe aright concerning the funda-
mental Articles of the Government to which I am
subject; to write, speak, and act on all Occasions
conformably to this Orthodox Faith, to oppose with
all the Powers of my Body and Mind, such as are
Enemies of our good Constitution, together with all
their secret and open Abettors, and to be obedient to
the King the supreme Magistrate of the Society.*

*Q. Rehearse unto me the Articles of thy Political
Creed?*

*A. I believe that the Supreme or Legislative Pow-
er of this Realm resides in the King, Lords, and
Commons; That his Majesty King George the Se-
cond is Sovereign or Supreme Executor of the Law,
to whom upon that account all Loyalty is due.
That each of the three Members of the Legislature
are endowed with their particular Rights, and Of-
fices; that the King by his Royal Prerogatives has
the Power of determining and appointing the Time
and Place of Meeting of Parliaments. That the
Consent of King, Lords, and Commons, is ne-
cessary to the Being of a Law, and all the three
make but one Lawgiver. That as to the Freedom
of Consent in making of Laws, those three Powers*

are

are independent, and that each and all the three are bound to observe the Laws that are made.

Q. Why is the Legislative Power Supreme ?

A. Because what gives Law to all, must be Supreme.

Q. What mean'st thou by Loyalty to the King ?

A. I have heard that Loy signifies Law ; and Loyalty, Obedience, according to Law ; therefore he who pays this Obedience is a loyal Subject, and he who executes the King's Command when contrary to Law is disloyal and a Traitor.

Q. Is it not a Maxim in the Law, that the King can do no Wrong ?

A. It is : For since Kings do not act immediately by themselves, but mediately by their Officers, and inferior Magistrates ; the Wisdom of the Law provides sufficiently against any undue Exercise of their Power, by charging all illegal Acts, and all kinds of Male-Administration upon their Ministers : by the great regard which is paid to the King by this Maxim, laying him under an indisputable Obligation, not to skreen his Ministers from Publick Justice or Publick Enquiry.

Q. What do'st thou mean by the Royal Prerogative ?

A. A Discretionary Power in the King to act for the Good of the People where the Laws are silent, never contrary to Law, and always subject to the Limitations of the Law.

Q. Doest thou owe no other Duty to the King but Obedience according to Law ?

A. Yes. I am bound to pray for him, to honour him, to behave myself respectfully towards him, and to speak respectfully of him, as it is written, Thou shalt not speak Evil of the Ruler of the People.

Q. Thou hast promised that in order to preserv this thy Liberty, thou wilt resist to the utmost of th Power the Enemies of our good Constitution ; who ar those Enemies ?

A. Su

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A. Such as deny the Title and Authority of the King who is acknowledg'd to be so by the Legislature : Such as by the Heretical Doctrines exalt the Royal Authority above the Laws : Such as endeavour to destroy the Authority and Independence of any of the three Members of the Legislature.

Q. How comes it that denying the Title and Authority of the King, who is acknowledged by the two Branches of the Legislature, is subverting a fundamental Law of the Constitution ?

A. Because if private Judgment is to be opposed to that of the Publick, there can be no Peace in that Society : Besides every Man in the Society is supposed to have given his Assent in that Matter already, for the Act of the Majority is the Act of every Individual.

Q. What are those Heretical Doctrines which exalt the King's Authority above the Laws.

A. Asserting, That there is something particularly Divine in Kingly Government, as being the first Government of the World, and appointed by God. And that there is in Kings an Authority and Hereditary Right of Succession independent of the Laws.

Q. How canst thou prove those to be heretical and false Doctrines ?

A. Because they are so far from being founded upon Scripture (as is pretended) that they are contrary to it. For first, It does not appear from Scripture how the first Political Societies were formed. Secondly, The first Government of God's People was not Monarchical; the Patriarchs were not Kings; the Government of the *Israelites* before *Saul's* Time was Republican; the People sent Ambassadors, *Joshua xxii.* the People in full Assembly demands Justice, *Judges xix and xx.* Thirdly, God Almighty gives a disadvantageous Character of Absolute

solute Monarchy, which see 2 Sam. viii. 4. If by God's Appointment, be meant a Divine Revelation or Mission, no Monarch upon Earth has it: If by God's Appointment be meant the Divine Authority, enjoyning Obedience to the lawful Ordinances of Man, the Supreme Power of a Commonwealth has it as much as a King: If by God's Appointment be meant God's Providence, a Robber, Tyrant, Usurper may be said to be so. Fifthly, There are several Passages in Scripture, that favour the Original Power of the People. Abraham demands a Burrying-place for Sarah of the People. The first Governors seem to have been Captains chosen for their Valour, by the People, *whoever will give Battle* (say the Princes and People of Gilead) *to the Children of Ammon, shall be Head over the Inheritance of Gilead*, accordingly *Jeptah* was chosen. God Almighty demands the Consent of the People even to his own Laws, accordingly Moses proposeth them in a full Assembly, and demands their Consent as to a Covenant, *See Deut. 5.* God Almighty condescended to this Natural Right of the People in changing the Form of their Government (tho' contrary to his Admonition) when they demanded a King to rule over them, and commands Samuel to *hearken to the Voice of the People*, 2 Sam. viii. There are many more Proofs of this Truth to be found in Scripture, by any Man who reads with Attention.

Q. Does not Conquest give a Right to absolute Monarchy?

A. No : For unjust Force can never give any just Dominion : And Conquest in a just War, gives the Conqueror absolute Dominion only over the Individuals he has subdued.

Q. What thinkest thou of Hereditary Right?

A. No

A. No Man can have Hereditary Right by the Title of King, for there are Kingdoms Elective ; several Kingdoms have different Customs and Laws in determining the Successions of their Monarchs ; those of *Britain* and *France* are different, and both from the Customs of some other Monarchies ; therefore there can be no Right of Succession but by the Laws of the Land, and accordingly by the Act of Settlement his present Majesty King *George* the Second has an Hereditary Right in himself and lineal Descendants, subject to the Limitations of the Law, a more authentick Deed for Hereditary Right, than can be produced by any Prince in the World.

Q. Is not then the King above the Laws ?

A. By no means : For the Intention of Government being the Security of the Lives, Liberties, and Properties, of the Members of the Community, they never can be supposed by the Law of Nature, to give an Arbitrary Power over their Persons and Estates. King, is a Title, which translated into several Languages, signifies a Magistrate with as many different Degrees of Power, as there are Kingdoms in the World, and he can have no Power but what is given him by Law ; yea, even the Supreme or Legislative Power, is bound by the Rules of Equity, to govern by Laws enacted, and published in due Form ; for what is not Legal is Arbitrary.

Q. How comes it that those who endeavour to destroy the Authority and Independance of any of the Branches of the Legislature, subvert the Constitution ?

A. By the fundamental Laws of the Constitution, the free and impartial Consent of each of the

three

three Members is necessary to the Being of a Law, therefore if the Consent of any of the Three is wilfully omitted, or obtain'd by Terror or Corruption, the Legislature is violated; and instead of three there may be really and effectually but one Branch of the Legislature.

Q. Can thou illustrate this by any Example.

A. The Royal Authority and that of the House of Peers were both destroyed by the House of Commons, and by a small Part of That, in the late Civil War; so that the very Form of Government was annihilated.

Q. Can you give me an Instance where the Form of Government may be kept, and yet the Constitution destroyed?

A. Yes. The Forms of the Free Government of Rome, were preserved under the Arbitrary Government of the Emperors: There was a Senate, Consuls, and Tribunes of the People; as one might say King, Lords, and Commons, and yet the Government under the Emperors was always Despotick, and often Tyrannical; and indeed the Worst of all Governments is Tyranny sanctify'd by the Appearance of Law.

Q. By what Means fell that great People into this State of Slavery?

A. I have read the Roman History, and by what I can judge, it was by Faction, Corruption, and Standing Armies.

Q. All That might happen to Romans; but did ever any Parliament of this Nation give up the Liberty of the Peop'e?

A. Yes: A Pack'd Parliament in Richard the Second's Time, established by a Law, the King's Arbitrary Power, and with Leave to name a Commission with Parliamentary Authority. Parliaments

liaments in *Henry the Eighth's* Time were Slaves to his Passions, and One gave the King a Legislative Authority. And there are many Instances of Parliaments making dangerous Steps towards the Destruction of the Liberty of the People.

Q. Who were the English Monarchs who were most indulgent to the Liberties of the People?

*A. The great King Alfred, who declar'd, That the English Nation was as free, as the Thoughts of Man. The glorious Monarchs, Edward the First, Edward the Third, and Henry the Fifth, who would not let his People swear to him till he had an Opportunity of swearing to them, at his Coronation. And the Immortal Queen Elizabeth, who declar'd it by Law, High Treason, during her Life, and a *Premunire* afterwards, to deny the Power of Parliament in limiting and binding the Descent or Inheritance of the Crown, or the Claim to it.*

Q. When were those slavish Maxims of Hereditary Indefeazable Right and Prerogative, superior to Law, first introduced?

A. In the Time of James the First; who by endeavouring to establish them, laid the Foundation of all the Miseries which have since happened to his Family; and it is the greatest Security to the present Branch of it, that such Doctrines which sow the Seeds of Jealousy between the King and his People, are by the present Establishment quite exploded.

Q. What dost thou learn from those Histories?

A. That a King of this Realm, in the full Possession of the Affections of his People is greater than any Arbitrary Prince, and that the Nation can never be effectually undone but by a wicked Parliament; and lastly, to be thankful to God that under our present most gracious King our Co

Constitution is preserv'd entire, tho' at the same time there are many Circumstances which call Loudly for Vigilance.

Q. What are those?

A. Such as have been the Fore-runners and Causes of the Loss of Liberty in other Countries, Decay of Virtue, and Publick Spirit, Luxury and Extravagance in Expence, Venality and Corruption, in private and publick Affairs.

Q. How comes there to be a Decay of Publick Spirit, when there is more than usual a Desire to serve The Publick?

A. If a Desire to live upon the Publick, be a Publick Spirit, there is enough of it at this Time, when Extravagance makes People crave more, and the Administration of a Publick Revenue (perhaps treble what it was before the Revolution) enables the Crown to give more than formerly.

Q. What doſt thou fear from this?

A. That such as serve the Crown for Reward, may in Time sacrifice the Interest of the Country to their Wants; that Greediness of publick Money may produce a flavish Complaisance as long as the Crown can pay; and Mutiny when it cannot; and in general, that Motives of Self-Interest will prove an improper and weak Foundation for our Duty to our King and Country.

Q. I much rejoice to see a Person of your Knowledge and Publick Spirit; therefore I ask you what is the Sum and Substance of the Virtue of a good Citizen?

A. The Love of our Country comprehends in it the Virtues of a good Citizen, as the Love of God those of a good Christian: It is the Love not only of One, but of Millions of Neighbours; not only of our Neighbours now living, but of them

and

and of their Posterity. It is an Instinct as well as Duty of Nature; the very Soil from which as from a common Mother, Mankind are nourish'd and the last common Repository of their dead Bodies, has been reputed amongst human Creatures, as a Bond of Union; *Joseph* comforted himself with his dying Breath, reflecting that his Bones should rest amongst his Bretheren. I read of one *Themistocles* who, tho' he had been banished from *Greece* and Hofpitality, and receiv'd in *Perſia*, ordered his Corps to be carried back and buried by stealth in his own Country. All Nations sink and rise in proportion as this Virtue prevails. When I read the *Roman* History I am transported with Joy, and a profound Reverence for those Worthies who sacrificed their Lives, and what was perhaps dearer to them, to the Love of their Country. Nor is our own Country destitute of Examples of such Heroick Virtue, of which some have transmitted the glorious Fruits to their Posterity; and such as have fail'd of that, have attain'd to a glorious Immortality, and advanc'd the Temporal Felicity of Generations past and to come. The Love of our Country is both a Moral and Religious Duty.

Q. How doſt thou prove That?

A. The Love which we owe to all Mankind, is not only allow'd but enjoin'd, in greater Degrees to particular Societies, whereof we are Members, as Nations, Neighbours, Kindred, Families, and Children: There are many Precepts of the Examples in Scripture enforcing this Duty of the Love of our Country; and holy Men of Old, as they were endowed with a religious, seem'd proportionably fill'd with a Publick Spirit; the *Old Testament* is full of such Examples: This was the shining Virtue of *Moses*, and of all the Captains, Princes, and Prophets;

Prophets of God's People. One of the Books of the Prophets is a Lamentation for the Captivity and Desolation of *Judah*; *Woe unto me* (said *Mathias*, 2 *Maccabees* ii.) *wherefore was I born, to see the Desolation of my People.* Then he and his Sons rent their Cloths and put on Sack-cloth and Mourning; *We are ready to die*, said the young Men, *rather than transgress the Laws of our Country.* It is said of *Judas Maccabeus*, *That he made the Jews bold and ready to die for the Laws of their Country.* This Virtue was more eminent in our Blessed Saviour than in any of the Sons of Men: He confin'd at first the Benefit of his Gospel and Miracles to his own Country; he heals the Centurion's Servant upon the Motive of his being a Friend to the Jewish Nation; and most tender in his Lamentation over the approaching Desolation of his Country, and his Intercession for it with his dying Breath. St. *Paul* could ev'n wish himself accursed for his Countrymen, his Brethren, and Kinsmen after the Flesh. And I am of Opinion, that the Decay of the Publick Spirit at this time is much owing to the Decay of Virtue, and that true Religion, which is always free from Bigotry and Superstition, and a persecuting Spirit.

Q. What wouldst thou do for thy Country?

A. I would die to procure its Prosperity: And I would rather that my Posterity were cut off, than that they should be Slaves; but as Providence at present requires none of those Sacrifices, I content myself to discharge the ordinary Duties of my Station, and to exhort my Neighbours to do the same.

Q. What are the Duties of your Station?

A. To endeavour as far as I am able, to preserve the publick Tranquillity; and as I am a Freeholder,

to give my Vote for the Candidate whom I judge most worthy to serve his Country : For if for any partial Motive I should give my Vote for one unworthy, I should think myself justly chargeable with his Guilt.

Q. Thou hast perhaps but one Vote of Five Hundred, and the Member perhaps one of Five Hundred more, then your share of the Guilt is but small?

A. As he who affists at a Murder is guilty of Murder, so he who acts the lowest Part in the Enslaving his Country, is guilty of a much greater Crime than Murder.

Q. Is Enslaving one's Country a greater Crime than Murder?

A. Yes: Inasmuch as the Murder of Human Nature is a greater Crime than the Murder of a Human Creature; or as he who debaseth and rendereth miserable the Race of Mankind, is more wicked than he who cutteth off an Individual.

Q. Why is Enslaving Mankind murdering Human Nature?

A. Because Mankind in a State of Slavery and Freedom is a different Sort of Creature; for Proof of this I have read what the Greeks were of old, and what they are now in a State of Slavery.

Q. What is become of the Heroes, Philosophers, Orators, and free Citizens of Greece?

A. They are now Slaves to the Great Turk.

Q. What is become of the Scipio's and Cato's of Rome?

A. They sing now on the English Stage.

Q. Does not the Tranquillity occasioned by absolute Monarchy make the Country thrive?

A. Peace and Plenty are not the genuine Fruits of absolute Monarchy; for absolute Monarchies are more subject to Convulsions, than free Governments.

ments, and Slavery turneth the fruitful Plains into a Desart ; whereas Liberty, like the Dew from Heaven, fructifieth the barren Mountains. This I have learn'd from Travellers, who have visited Countries in both Conditions ; therefore as I said before, I should reckon myself guilty of the greatest Crime human Nature is capable of, if I were any ways accessary to the enslaving my Country ; tho' I have but one Vote, many Unites make a Number, and if every Elector should Reason after the same manner, that he has but one ; what must become of the whole ? a Law of great Consequence, and the Election of the Member who voteth for that Law, may be both carried by one Vote ; great and important Services for the Liberties of their Country, have been done by ordinary Men : I have read, that the Institution of the Tribunes of *Rome*, or the whole Power of the Commons, was owing to a Word spoke in season by a common Man.

Q. Is it not lawful then to take a Bribe from a Person otherwise worthy, to serve his Country?

A. No more than for a Judge to take a Bribe for a Righteous Sentence ; nor is it any more lawful to corrupt, than to commit Evil that Good may come of it : Corruption converts a good Action into Wickednes. Bribery of all Sorts is contrary to the Law of God ; it is a heinous Sin, often punished with the severest Judgmens ; it involves in it the Sin of Perjury as the Law stands now, and besides the greatest Folly and Madnes.

Q. How is it contrary to the Law of God ?

A. The Law of God saith expressly, *Thou shall not wrest Judgment ; Thou shalt not take a Gift :* If it is a Sin in a Judge, it is much more in a Law-giver

giver, or an Elector; because the Mischiefs occasioned by the first reach only to Individuals, that of the last may affect whole Nations, and even the Generations to come. The Psalmist describing the Wicked, saith, *bis right Hand is full of Bribes*: The Prophet describing the Righteous, tells us, *he shaketh his Hands from holding a Bribe*: Samuel justifying his Innocence, appeals to the People, *of whose Hands have I taken a Bribe?* Then as to divine Vengeance, holy Job tells us, *that God shall destroy the Tabernacle of Bribery*. Achan's Avarice who had appropriated to his own Use the golden Wedge and the Babylonish Garment, brought the Judgments of God upon the whole People, so that they fled before their Enemies, till the Criminal was discovered and stoned to Death. The Leprosy adhered to Gehazi (the Servant of Elisa) and his House for ever, for taking a Bribe from Naaman, a rich Minister of a great Prince: Therefore he that taketh a Bribe may justly expect what is threatned in Holy Writ; *He shall not prosper in his Way, neither shall his Substance continue; his Silver and Gold shall not be able to deliver him in the Day of the Wrath of the Lord.*

Q. Why is he that taketh a Bribe guilty of the Sin of Perjury?

A. Because he sweareth,

I A. B. do swear (or being one of the People called Quakers, I A. B. do solemnly affirm) I have not receiv'd, nor had by my Self, or any Person whatsoever in Trust for me, or for my Use and Benefit, directly or indirectly, any Sum or Sums of Money, Office, Place, or Employment, Gift, or Reward, or any Promise or Security for any Money, Office, Employment, or Gift, in order to give my Vote at this Election, and that I have not before been polled at this Election.

B

Q. What

Q. What thinkest thou of those who are bribed by Gluttony and Drunkenness.

A. That they are viler than Esau who sold his Birth-right for a Mess of Porridge.

Q. Why is taking a Bribe Folly or Madness?

A. Because I must refund Ten-fold in Taxes of what I take in Election; and the Member who bought me, has a fair Pretence to sell me, nor can I in such a Case have any just Cause of Complaint.

Q. What wilt thou say then to the Candidate that offers thee a Bribe?

A. I will say, " Thy Money perish with thee ; " " as thou art now purchasing thy Seat in Parliament, I have just Reason to suspect that thou " resolvest to sell thy Vote ; what thou offerest " and what thou promisest may be the Price of " the Liberty of my Country : I will not only " reject thy Bribe with Disdain, but will vote " against thee.

Q. Is not the Justice of a King, sufficient Security for the Liberty of the People?

A. The People ought to have more Security for all that is valuable in the World, than the Will of a mortal and fallible Man ; a King of Britain may make as many Peers, and such, as he pleaseth ; therefore the last and best Security for the Liberties of the People, is a House of Commons Genuine and Independant.

Q. What meanest thou by a Genuine House of Commons ?

A. One that is the lawful Issue of the People, and no Bastard.

Q. How is a Bastard House of Commons produc'd ?

A. Whe

A. When the People by Terror, Corruption, or other indirect Means, chuse such as they otherwise would not chuse; when such as are fairly chosen, are not returned; when such as are returned, are turn'd out by partial Votes in controverted Elections, and others not fairly chosen set in their Places.

Q. *How may a House of Commons become dependent?*

A. When the Freedom of Voting is destroy'd by Threatnings, Promises, Punishments, and Rewards by the open Force of the Government, or the Insults of the Populace; but above all by private Influence; for they who are armed with the Power of the Crown, have many ways of gratifying such as are subservient to their Designs, and many ways of oppressing such as oppose them, both within the Bounds of the Law.

Q. *Can a King have a more faithful Council than a House of Commons, which speaketh the Sense of the People?*

A. None: For they will not only give him impartial Council, but will powerfully and chearfully assist him to execute what they advise.

Q. *What are the Marks of a Person worthy to serve his Country in Parliament?*

A. The Marks of a good Ruler given in Scripture, will serve for a Parliament-man; Such as rule over you shall be Men of Truth, hating Covetousness, they shall not take a Gift, they shall not be afraid of the Face of a Man, Deut. xvi. therefore I conclude, That the Marks of a good Parliament-man are Riches with Frugality, Integrity, Courage, being well affected to the Constitution, Knowledge of the State of the Country, being prudently frugal of the Money, careful of the Trade, and zealous over the Liberties of the People, having stuck to the Interests

of their Country in perilous Times, and being assiduous in attendance.

Q. Who is most likely to take a Bribe?

A. He who off'reth one.

Q. Who is likely to be frugal of the People's Money?

A. He who puts none of it in his own Pocket.

Q. You seem by this to be averse from chusing such as accept of Places and Gratuities from the Crown, what is your Reason for this Partiality?

A. I am far from thinking that a Man may not serve his King, and Country faithfully at the same time: nay their Interests are inseparable. Mr. Such-an-one, my Lord's Steward is a very honest Man, and yet if I had any Affairs to settle with my Lord, I would chuse my Neighbour for a Referree rather than my Lord's Steward.

Q. Why is Frugality of the People's Money so necessary at this time?

A. Because they have run out much, and are still much in Debt: My Father and I have paid our share of One Hundred Millions, and I have heard there are near Fifty more to pay: I grudge not this prodigious Expence, as far as it has been the necessary Price of Liberty; but as it would grieve me much to see this Blessing ravish'd from me which has cost me so dear; so on the other hand I think it expedient to save, now the Affair is over, and the Government settled.

Q. Who are those who are careful of the Trade of the Nation?

A. Such as are willing to keep it free from all vexatious Interruptions by Inspections, Entering into Houses, Seizures, Suits, and the Oppression of Tax-gatherers, as much as possible; such as are willing to take off the burdensome Duties which encrease

increase the Expence of the Workman, and consequently the Price of our Manufactures.

Q. But as you have a Freehold, would you not be willing to be excus'd from paying two Shillings in the Pound by laying Excises upon other Parts of our Consumptions?

A. No doubt but every Landed Man would be glad to be free from paying Two Shillings in the Pound ; but at the same time I would not raise by another Tax Two Shillings in the Pound, nor One Shilling in the Pound for a Perpetuity. For Parliaments who haye no more to give, may be disappointed in the Redress of their Grievances. Besides, I would not be deluded by an Impossibility ; for if my Tenant has any new Tax laid upon him, I am afraid he will not pay me so much Rent ; so that the new Tax must still affect Land. Then it is utterly impossible to raise by Excises what shall be equivalent to Two Shillings in the Pound without the Ruin of Trade ; for the Excises which are settled already, generally speaking, raise double the Duty upon the People, of what they bring into the Government.

Q. How canst thou prove that ?

A. By Experience of several Excises, as of Leather, Candles, Soap, &c. Whatever is brought into the Publick by those Excises, is raised double upon the People ; therefore if a Million of Money, or what is equivalent to Two Shillings in the Pound, were levy'd by Excise, it would be Two Millions upon the Excis'd Commodities, which must destroy every Subject of Trade in Britain.

Q. Why do'st thou insist, That a Knowledge of the State of the Country is a necessary Qualification for a Parliament-man ?

A. Because this is a Qualification, of late, very

B. 3 much

much unheeded : I have heard that there are many Corporations that never saw their Members.

Q. Is then a Writ of Parliament only a Conge d'Election for a Bishop, where the King nominates ?

A. God forbid ; the Crown is never to meddle in an Election.

Q. Why is assiduous Attendance so necessary ?

A. Because a Parliament-man is entrusted with the Lives, Liberties and Properties of the People, which have often been endangered by the Non-attendance of many Members ; because if Representatives do not attend, I may have a Law impos'd upon me, to which I had no opportunity of giving my Assent.

Q. Thou hast prudently and justly resolv'd to promote, to the utmost of thy Power, the Publick Tranquillity ; what are the Advantages thou proposest from that ?

A. All the Advantages resulting from Political Society depend upon the Publick Tranquillity : Besides, by Publick Tranquillity, Armies, which are the Mark of Distrust of the Affections of the People, may be Disbanded.

Q. Why don't thou not have Armies in Time of Peace ?

A. Because Armies have overturn'd the Liberties of most Countries ; and all who are well affected to Liberty, ever hated them ; because they are subject to an implicit Obedience to their Officers, and to a Law of their own ; because they are so many lusty Men taken from Work, and maintain'd at an extravagant Expence upon the Labour of the rest ; because they are many Ways burdensome to the People in their Quarters even under the best Discipline, especially in dear Countries ; because there are so many more Preferments in the Hands of Designing

signing Ministers ; and lastly, because the King will never be deny'd an Army as great as he pleaseth, when it is necessary.

Q. Thou rightly judgest of thy Happiness in being a Member of a Political Society, govern'd by Laws, to which the People give their Consent : Thou hast been likewise well instructed in the fundamental Laws of the Government, and art well aware of the wicked and abominable Practices that undermine, and are likely to overturn the Constitution : Be thou likewise verily persuaded that the equitable and fundamental Laws of a Nation are, in a sound Sense, stamp'd with a Divine Authority ; and that the good Order, Peace, and Happiness of the Society is firmly connected with a strict Observance of them. That the Prosperity of Nations depend upon their Virtue, not only as an effect upon its Natural Cause, but by the immutable Appointment of Divine Justice, by which Political Societies must receive their Rewards and Punishments in this World, since they have no Being in the next ; consequently the Threatnings and Promises which occur in the Old Testament are, in a proper Sense, as applicable to other Nations as the Israelites, therefore thou and all the People of this Land may suppose that God Almighty speaketh to them as he spoke by Moses unto the Israelites, Deut. xxviii. 1. And it shall come to pass, if thou shalt hearken diligently unto the Voice of the Lord thy God, to observe and do all his Commandments, (that is the Laws of their Constitution) which I command thee this Day ; that the Lord thy God will set thee on high above all Nations of the Earth, &c. Verse 15. But it shall come to pass, if thou wilt not hearken unto the Voice of the Lord thy God, to observe to do all his Commandments and his Statutes which I command thee this Day ; that all these Curses shall come upon thee

thee and overtake thee. Cursed shalt thou be in the City, and Cursed shalt thou be in the Field. Cursed shall be thy Basket and thy Store. Cursed shall be the Fruit of thy Body, and the Fruit of thy Land, the Increase of thy Kine, and the Flocks of thy Sheep. Cursed shalt thou be when thou comest in, and Cursed shalt thou be when thou goest out, &c. &c.



ΓΝΩΘΙ ΣΕ'ΑΤΤΟΝ. Know Yourself.

WHAT am I? how produc'd? and for what end?
Whence drew I being? to what period tend?
Am I th'abandon'd orphan of blind chance;
Dropt by wild atoms in disorder'd dance?
Or from an endless chain of causes wrought?
And of unthinking substance, born with thought?
By motion which began without a cause,
Supreamly wise, without design or laws,
Am I but what I seem, mere flesh and blood;
A branching channel, with a mazy flood?
The purple stream that through my vessels glides,
Dull and unconscious flows like common tides:
The pipes through which the circling juices stray,
Are not that thinking I, no more than they:
This frame, compacted with transcendent skill,
Of moving joints obedient to my will;
Nurs'd from the fruitful glebe, like yonder tree,
Waxes and wastes; I call it mine, not me:
New matter still the mould'ring mass sustains,
The mansion chang'd, the tenant still remains;

And

And from the fleeting stream repair'd by food,
Diftin&t, as is the swimmer from the flood.
What am I then? sure, of a nobler birth,
Thy parents right, I own a mother, earth;
But claim superior lineage by my SIRE,
Who warm'd th'unthinking clod with heavenly fire:
Essence divine, with lifeless clay allay'd,
By double nature, double instinct sway'd;
With look erect, I dart my longing eye,
Seem wing'd to part, and gain my native sky;
I strive to mount, but strive, alas! in vain,
Ty'd to this mafly globe with magick chain.
Now with swift thought I range from pole to pole,
View worlds around their flaming centers roll:
What steady powers their endless motions guide,
Thro' the same trackless paths of boundlets void!
I trace the blazing comet's fiery trail,
And weigh the whirling planets in a scale:
Those godlike thoughts, while eager I pursue,
Some glitt'ring trifle offer'd to my view,
A gnat, an insect, of the meanest kind,
Erase the new-born image from my mind;
Some beastly want, craving, importunate,
Vile as the grinning mastiffs at my gate,
Calls off from heav'nly truth this reas'ning me,
And tells me I'm a brute as much as he.
If on sublimer wings of love and praise,
My soul above the starry vault I raise,
Lur'd by some vain conceit, or shameful lust,
I flag, I drop, and flutter in the dust.
The tow'ring lark thus from her lofty strain,
Stoops to an emmet, or a barley grain.
By adverse gusts of jarring instincts tost,
I rove to one, now to the other coast;
To blifs unknown my lofty soul aspires,
My lot unequal to my vast desires.

As 'mongst the hinds a child of royal birth
 Finds his high pedigree by conscious worth ;
 So man, amongst his fellow brutes expos'd,
 Sees he's a king, but 'tis a king depos'd :
 Pity him, beasts ! you by no law confin'd,
 Are barr'd from devious paths by being blind ;
 Whilst man, through op'ning views of various ways
 Confounded, by the aid of knowledge strays ;
 Too weak to choose, yet choosing still in haste,
 One moment gives the pleasure and distaste ;
 Bilk'd by past minutes, while the present cloy,
 The flatt'ring future still must give the joy.
 Not happy, but amus'd upon the road,
 And (like you) thoughtless of his last abode,
 Whether next sun his being shall restrain,
 To endless nothing, happiness, or pain.

Around me, lo, the thinking thoughtless crew,
 (Bewilder'd each) their different paths pursue ;
 Of them I ask the way ; the first replies,
 Thou art a god ; and sends me to the skies.
 Down on this turf (the next) thou two-legg'd beast,
 There fix thy lot, thy bliss, and endless rest :
 Between those wide extremes the length is such,
 I find I know too little or too much.

“ Almighty pow'r, by whose most wise command,
 “ Helpless, forlorn, uncertain here I stand ;
 “ Take this faint glimmering of thy self away,
 “ Or break into my soul with perfect day !
 This said, expanded lay the sacred text,
 The balm, the light, the guide of souls perplext :
 Thus the benighted traveller that strays
 Through doubtful paths, enjoys the morning rays ;
 The nightly mist, and thick descending dew,
 Parting, unfold the fields, and vaulted blue.
 “ O truth divine ! enlightened by thy ray,
 “ I grope and guess no more, but see my way ;

“ Thou

“ Thou cleared’st the secret of my high descent,
 “ And told me what those mystic tokens meant ;
 “ Marks of my birth, which I had worn in vain,
 “ Too hard for worldly sages to explain ;
 “ Zeno’s were vain, vain Epicurus’ schemes,
 “ Their systems false, delusive were their dreams ;
 “ Unskill’d my twofold nature to divide,
 “ One nurs’d by pleasure, and one nurs’d by pride :
 “ Those jarring truths which human art beguile ;
 “ Thy sacred page thus bid me reconcile.

Offspring of God, no less thy pedigree,
 What thou once wer’t, art now, and still may be, }
 Thy God alone can tell, alone decree ;

Faultless thou dropt from his unerring skill,
 With the bare pow’r to sin, since free of will :
 Yet charge not with thy guilt, his bounteous love,
 For who has power to walk, has power to rove ;
 Who acts by force impell’d, can nought deserve ;
 And wisdom short of infinite, may swerve.

Born on thy new-imp’d wings, thou took’st thy flight,
 Left thy creator, and the realms of light ;
 Disdain’d his gentle precept to fulfil ;

And thought to grow a god by doing ill :
 Though by foul guilt thy heav’nly form defac’d,
 In nature chang’d from happy mansions char’d,
 Thou still retain’st some sparks of heav’nly fire,
 Too faint to mount, yet restless to aspire ;

Angel enough to seek thy bliss again,
 And brute enough to make thy search in vain.

The creatures now withdraw their kindly use,
 Some fly thee, some torment, and some seduce ;
 Repast ill suited to such diff’rent guests,
 For what thy sense desires, thy soul distastes ;
 Thy lust, thy curiosity, thy pride,
 Curb’d, or deferr’d, or balk’d, or gratify’d,

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Rage on, and make thee equally unbless'd,
In what thou want'st, and what thou hast possest;
In vain thou hop'st for bliss on this poor clod,
Return, and seek thy father, and thy God :
Yet think not to regain thy native sky,
Born on the wings of vain philosophy ;
Mysterious passage ! hid from human eyes ;
Soaring you'll sink, and sinking you will rise :
Let humble thoughts thy wary footsteps guide,
Regain by meekness what you lost by pride.


HUYGENS de Ratiociniis in Ludo Aleæ :

Translated into English by Dr. ARBUTHNOT.

The P R E F A C E .

I T is thought as necessary to write a Preface before a Book, as it is judg'd civil, when you invite a Friend to Dinner, to proffer him a Glass of Hock beforehand for a Whet : And this being maim'd enough for want of a Dedication, I am resolv'd it shall not want an Epistle to the Reader too. I shall not take upon me to determine, whether it is lawful to play at Dice or not, leaving that to be disputed betwixt the Fanatick Parsons and the Sharpers ; I am sure it is lawful to deal with Dice as with other Epidemic Distempers ; and I am confident that the writing a Book about it, will contribute as little towards its Encouragement, as Fluxing and Precipitates do to Whoring.

It will be to little purpose to tell my Reader, of how great Antiquity the playing at Dice is, I will only let him know, that by the Aleæ Ludus, the Antients comprehended all Games, which were subjected to the

Determina-

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Determination of mere Chance; this sort of Gaming was strictly forbid by the Emperor Justinian, Cod. Lib. 3. Tit. 43. under very severe Penalties; and Phocius Nomocan. Tit. 9. Cap. 27. acquaints us, that the Use of this was altogether denied the Clergy of that time. Seneca says very well, Aleator quantum in arte est melior, tantum est nequior; That by how much the one is more skilful in Games, by so much he is the more culpable; or we may say of this, as an ingenious Man says of Dancing, that to be extraordinary good at it, is to be excellent in a Fault; therefore I hope no body will imagine I had so mean a Design in this, as to teach the Art of Playing at Dice.

A great part of this Discourse is a Translation from Mons. Huygens's Treatise, De ratiociniis in ludo Aleæ; one, who in his Improvements of Philosophy, has but, one Superior, and I think few or no Equals. The whole I undertook for my own Divertissement, next to the Satisfaction of some Friends, who would now and then be wrangling about the Proportions of Hazards in some Cases that are here decided. All it required was a few spare Hours, and but little Work for the Brain; my Design in publishing it, was to make it of more general Use, and perhaps persuade a raw Squire, by it, to keep his Money in his Pocket; and if, upon this account, I should incur the Clamours of the Sharpers, I do not much regard it, since they are a sort of People the World is not bound to provide for.

You will find here a very plain and easy Method of the Calculation of the Hazards of Game, which a Man may understand, without knowing the Quadratures of Curves, the Doctrine of Series's, or the Laws of Concentripetation of Bodies, or the Periods of the Satellites of Jupiter; yea, without so much as the Elements of Euclid. There is nothing required for the comprehending the whole, but common Sense and practical

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tical Arithmetick; saving a few Touches of Algebra, as in the first Threes Propositions, where the Reader, without suspicion of Popery, may make use of a strong implicit Faith; tho' I must confess, it does not much recommend itself to me in these Purposes; for I had rather he would enquire, and I believe he will find the Speculation not unpleasant.

Every Man's Success in any Affair is proportional to his Conduct and Fortune. Fortune (in the sense of most People) signifies an Event which depends on Chance, agreeing with my Wish; and Misfortune signifies such an one, whose immediate Causes I don't know, and consequently can neither foretel nor produce it (for it is no Heresy to believe, that Providence suffers ordinary matters to run in the Channel of second Causes). Now I suppose, that all a wise Man can do in such a Case is, to lay his Business on such Events, as have the most powerful second Causes, and this is true both in the great Events of the World, and in ordinary Games. It is impossible for a Die, with such determined force and direction which makes it fall on such a determined side, only I don't know the force and direction which makes it fall on such a determin'd side, and therefore I call that Chance, which is nothing but want of Art; that only which is left to me, is to wager where there are the greatest number of Chances, and consequently the greatest probability to gain; and the whole Art of Gaming, where there is any thing of Hazard, will be reduced to this at last, viz. in dubious Cases to calculate on which side there are most Chances; and tho' this can't be done in the midst of Game precisely to an Unit, yet a Man who knows the Principles, may make such a Conjecture, as will be a sufficient direction to him; and tho' it is possible if there are any Chances against him at all, that he may lose, yet when he chuseth the safest

side,

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side, he may part with his Money with more content (if there can be any at all) in such a Case.

I will not debate, whether one may engage another in a disadvantageous Wager. Games may be suppos'd to be a tryal of Wit as well as Fortune, and every Man, when he enters the Lists with another, unless out of Complaisance, takes it for granted, his Fortune and Judgment are, at least, equal to those of his Play-Fellows; but this I am sure of, that false Dice, Tricks of Leger-de-main, &c. are inexcusables, for the question in Gaming is not, Who is the best Jugler?

The Reader may here observe the Force of Numbers, which can be successfully applied, even to those things, which one would imagine are subject to no Rules. There are very few things which we know, which are not capable of being reduc'd to a Mathematical Reasoning; and when they cannot, it's a sign the Knowledge of them is very small and confus'd; and where a Mathematical reasoning can be had, it's as great folly to make use of any other, as to grope for a thing in the Dark, when you have a Candle standing by you. I believe the Calculation of the Quantity of Probability might be improved to a very useful and pleasant Speculation, and applied to a great many Events which are accidental, besides those of Games; only these Cases would be infinitely more confus'd, as depending on Chances which the most part of Men are ignorant of; and as I have hinted already, all the Politicks in the World, are nothing else but a kind of Analysis of the Quantity of Probability in casual Events, and a good Politician signifies no more, but one who is dextrous at such Calculations; only the Principles which are made use of in the Solution of such Problems, can't be studied in a Closet, but acquired by the Observation of Mankind.

There is likewise a Calculation of the Quantity of Probability founded on Experience, to be made use of in

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in Wagers about any thing ; it is odds if a Woman is with Child, but it shall be a Boy ; and if you would know the just odds, you must consider the Proportion in the Bills that the Males bear to the Females : The Yearly Bills of Mortality are observed to bear such Proportion to the live People as 1 to 30, or 26; therefore it is an even Wager, that one of thirteen, dies within a Year (which may be a good Reason, tho' not the true, of that foolish piece of Superstition,) because, at this rate, if 1 out of 26 dies, you are no loser. It is but 1 to 18 if you meet a Parson in the Street, that he proves to be a Non-Juror, because there is but 1 of 36 that are such. It is hardly 1 to 10, that a Woman of Twenty Years old has her Maiden-head, and almost the same Wager, that a Town-Spark of that Age has not been clap'd. I think a Man might venture some odds, that 100 of the Gens d'arms beats an equal Number of Dutch Troopers ; and that an English Regiment stands its ground as long as another, making Experience our Guide in all these Cases and others of the like Nature.

But there are no casual Events, which are so easily subjected to Numbers, as those of Games ; and I believe, there the Speculation might be improved so far, as to bring in the Doctrine of the Series's and Logarithms. Since Gaming is become a Trade, I think it fit the Adventurers should be upon the Square ; and therefore in the Contrivance of Games there ought to be a strict Calculation made use of, that they mayn't put one Party in more probability to gain, than another ; and likewise, if a Man has a considerable Venture ; he ought to be allowed to withdraw his Money when he pleases, paying according to the Circumstances he is then in : And it were easy in most Games to make Tables, by inspection of which, a Man might know what he was either to pay or receive, in any Circumstances

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stances be is then in : And it were easy in most Games to make Tables, by Inspection of which, a Man might know what he was either to pay or receive, in any Circumstances you can imagine, it being convenient to save a part of one's Money, rather than venture the loss of it all.

I shall add no more, but that a Mathematician will easily perceive, it is not put in such a Dress as to be taken notice of by him, there being abundance of Words spent to make the more ordinary sort of People understand it.

FOR the sake of those who are not vers'd in Mathematics, I have added the following Explanation of Signs. = Equal. + More, or to be added. — Less, or to be subtracted. × Multiplied. ÷ Divided. Example, $3 \times 4 + 3 - 1 = 15 = \frac{5}{9}a$, is to be read thus ; 3 multiplied in 4, more by 3, less by 1, is equal to 14, which is equal to 5 ninth parts of a.

ALTHO' the Events of Games, which Fortune solely governs, are uncertain, yet it may be certainly determin'd, how much one is more ready to lose than gain. For Example : If one should wager, at the first throw with one Die, to throw six, it's an accident if he gains or not ; but by how much it's more probable he will lose than gain, is really determin'd by the Nature of the Thing, and capable of a strict Calculation. So likewise if I should play with another on this Condition, that the Victory should be to the three first Games, and I had gain'd one already, it is still uncertain who shall gain the third ; yet by a demonstrative

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Reasoning, I can estimate both the Value of his Expectation and mine, and consequently (if we agree to leave the Game imperfect) determine how great a share of the Stakes belong to me, and how much to my Play-fellow; or if any were desirous to take my Place, at any rate I ought to sell it. Hence may arise innumerable Queries among two, three, or more Gamesters: And since the Calculation of these things is a little out of the common Road, and can be oft-times apply'd to good Purpose, I shall briefly here shew how it is to be done, and afterwards explain those things which belong properly to the Dice.

In both Cases I shall make use of this Principle, *One's Hazard or Expectation to gain any thing, is worth so much, as, if he had it, he could purchase the like Hazard or Expectation again in a just and equal Game.*

For Example, if one, without my Knowledge, should hide in one hand 7 Shillings, and in his other 3 Shillings, and put it to my choice which Hand I would take, I say this is as much worth to me, as if he should give me 5 Shillings; because, if I have 5 Shillings, I can purchase as good a Chance again, and that in a fair and just Game.

Prop. I. If I expect a or b, either of which, with equal probability, may fall to me, then my Expectation is worth a+b, that is, the half Sum of a and b.

THAT I may not only demonstrate, but likewise investigate this Rule, suppose the Value of my Expectation be x ; by the former Principle having x , I can purchase as good an Expectation again in a fair and just Game. Suppose then I play with another on these terms, That every one stakes

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x , and the Gainer give to the Loser a , this Game is just, and it appears, that at this rate, I have an equal hazard either to get a if I lose the Game, or $2x-a$ if I gain; for in this case I get $2x$, which are the Stakes, out of which I must pay the other a ; but if $2x-a$ were worth b , then I have an equal hazard to get a or b ; therefore making $2x-a=b$, $x=\frac{a+b}{2}$ which is the Value of my Expectation. The

Demonstration is easy; for having $\frac{a+b}{2}$, I can

play with another who will stake $\frac{a+b}{2}$ against it, on this Condition, that the Gainer should give to the Loser a ; by this means I have an equal Expectation to get a if I lose, or b if I win; for in the last case I get $a+b$ the Stakes, out of which I must pay a to my Play fellow.

In Numbers: if I had an equal hazard to get 3 or 7, then by this Proposition, my Expectation is worth 5, and it is certain, having 5, I may have the same Chance; for if I play with another, so that every one stakes 5, and the Gainer pay to the Loser 3, this is a fair way of gaming; and it is evident I have an equal hazard to get 3 if I lose, or 7 if I gain.

Prop. II. If I expect a , b , or c , either of which, with equal facility, may happen, then the Value of my Expectation is $\frac{a+b+c}{3}$, or the third part of the Sum of a , b , and c .

FOR the Investigation of which, suppose x be the value of my Expectation; then x must be such, as I can purchase with it the same Expectation in a just Game: Suppose the Conditions of the Game

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be, that playing with two others, each of us stak x , and I bargain with one of the Gamesters, if I wi to give him b , and he shall do the same to me ; b with the other, that if I gain, I shall give him c , au vice versa ; this is fair play : And here I have an equ hazard to get b , if the first win, c if the second, $3x - b - c$ if I gain myself; for then I get $3x$, viz. the Stakes, of which I give the one b and the other c but if $3x - b - c$ be equal to a , I have an equ Expectation of a , b , or c ; therefore making $3x - b - c = a$, $x = \frac{a + b + c}{3}$, which is the Value my Expectation. After the same Method you w find, if I had an equal hazard to get a , b , c , or the Value of my Expectation $\frac{a + b + c + d}{4}$, that the fourth part of the Sum of a , b , c , and d , &c.

Prop. III. *If the number of Chances, by which a falls me, be p, and the number of Chances, by which falls, be q, and supposing all the Chances do happen with equal facility, then the Value of my Expectation is $\frac{pa + bq}{p + q}$; i. e. the Product of a multiplied in the number of its Chances added to the Product of b multiplied into the number of its Chances, and the Sum divided by the number of Chances both of a and b.*

Suppose, as before, x be the Value of my Expectation ; then if I have x , I must be able to purchase with it that same Expectation again in fair Game : For this I shall take as many Play-felows as, with me, make up the number of $p + q$ of which let every one stake x , so the whole Stake will be $px + qx$, and every one plays with equi hopes of winning ; with as many of my Fellow Game

Gamesters as the Number q stands for, I make the bargain one by one, that whoever of them gains shall give me b , and if I win, I shall do so to them ; with every one of the rest of the Gamesters, whose Number is $p - 1$, I make this bargain, that whoever of them gains, shall give me a , and I shall give every one of them as much, if I gain : It's evident this is fair play ; for no Man here is injur'd ; and in this case I have q Expectations to gain b , and $p - 1$ Expectations to gain a , and 1 Expectation (*viz.* when I win myself) to get $px + qx - bq - ap + a$; for then I am to deliver b to every one of the q Players, and a to every one of the $p - 1$ Gamesters, which makes $qb + pa - a$; if therefore $qx + bx - bq - ap + a$ were equal to a , I would have p Expectations of a (since just now I had $p - 1$ Expectations of it) and q Expectations of b , and so would have just come to my first Expectation ; therefore putting $px + qx - bq - ap + a = a$, and then is $x = \frac{ap + bq}{p + q}$.

In Numbers : If I had 3 Chances to gain for 13, and 2 for 8, by this Rule, my hazard is worth 11 ; for 13 multiplied by 3 gives 39, and 8 by 2, 16, these two added, make 55, divided by 5 is 11 ; and I can easily shew, if I have 11, I can come to the like Expectation again ; for playing with four others, and every one of us staking 11, with two of them I make this bargain, that whoever gains shall give me 8, and I shall too so to them ; with the other two I make this bargain, that whoever gains shall give me 13, and I them as much if I gain, and 3 Expectations to get 13, *viz.* if either I or any of the other two gain ; for in this case I gain the Stakes, which are 55, out of which I am oblig'd to give the first

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two 8, and the other two 13, and so there remains 13 for myself.

Prop. IV. *That I may come to the Question propos'd, viz. The making a just Distribution amongst Gamesters, when their Hazards are unequal; we must begin with the most easy Cases.*

Suppose then I play with another, on condition that he who wins the three first Games shall have the Stakes, and that I have already gain'd two, I would know if we agree to break off the Game, and part the Stakes justly, how much falls to my share.

The first thing we must consider in such Questions is the number of Games that are wanting to both: For Example, if it had been agreed betwixt us, that he should have the Stakes who gain'd the first 20 Games, and if I had gain'd already 19, and my Fellow-Gamester but 18, my hazard is as much better than his in that case, as in this proposed, viz. When of 3 Games I have 2, and he but one, because in both cases there's 2 wanting to him, and 1 to me.

In the next place, to find the portion of the Stakes due to each of us, we must consider what would happen if the Game went on; it is certain, if I gain the first Game, I get the Stake, which I call a ; but if he gain'd, both our Lots would be equal, and so there would fall to each of us $\frac{1}{2}a$; but since I have an equal hazard to gain or lose the first Game, I have an equal Expectation to gain a , or $\frac{1}{2}a$, which, by the first Proposition, is as much worth as the half Sum of both; i. e. $\frac{1}{2}a$, so there is left to my Fellow-Gamester $\frac{1}{2}a$; from whence it follows, that he who would buy my Game ought to pay me for it $\frac{1}{2}a$; and therefore, he who undertakes

to gain one Game before another gains two, may wager 3 to 1.

Prop. V. Suppose I want but one Game, and my Fellow-Gamester three, it is required to make a just Distribution of the Stake.

LET us here likewise consider in what state we should be, if I or he gain'd the first Game; if I gain, I have the Stake a , if he, then he wants yet 2 Games, and I but 1, and therefore we should be in the same Condition which is supposed in the former Proposition; and so there would fall to my Share, as was demonstrated there, $\frac{3}{4}a$; therefore with equal facility there may happen to me a , or $\frac{3}{4}a$, which, by the first Proposition, is worth $\frac{7}{8}a$, and to my Fellow-Gamester there is left $\frac{1}{8}a$, and therefore my hazard to his is as 7 to 1.

As the Calculation of the former Proposition was requisite for this, so this will serve for the following. If I should suppose myself to want but one Game, and my Fellow four, (by the same Method) you will find $\frac{11}{16}$ of the Stake belongs to me, and $\frac{5}{16}$ to him.

Prop. VI. Suppose I want two Games, and my Fellow Gamester three.

THEN by the next Game it will happen that I want but one, and he three, which (by the preceeding Proposition) is worth $\frac{7}{8}a$; or that we should both want two, whence there will be $\frac{1}{2}a$ due to each of us: Now I being in an equal probability to gain or lose the next Game, I have an equal hazard to gain $\frac{7}{8}a$ or $\frac{1}{2}a$, which by the first Proposition is worth $\frac{11}{16}a$; and so there are eleven parts of the Stakes due to me, and five to my Fellow.

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PROP. VII. *Let us suppose I want two Games, and my Fellow four.*

IF I gain the next Game, then I shall want but one, and my Fellow four; but if I lose it, then I shall want two, and he three: So I have an equal hazard for gaining $\frac{1}{2}a$, or $\frac{1}{3}a$, which, by the first is worth $\frac{1}{3}a$: So it appears, that he who is to gain two Games for the other's four, is in a better Condition than he who is to gain one for the other's two; for my share in the first case is $\frac{1}{2}a$ or $\frac{1}{3}a$, which is less than $\frac{1}{3}a$, my share in the last.

PROP. VIII. *Let us suppose three Gamesters, whereof the first and second want 1 Game, but the third 2.*

TO find the share of the first, we must consider what would happen if either he, or any of the other two gain'd the first Game; if he gains, then ne has the Stake a ; if the second gain, he has nothing; but if the third gain, then each of them would want a Game, and so $\frac{1}{2}a$ would be due to every one of them. Thus the first Gamester has one Expectation to gain a , one to gain nothing, and one for $\frac{1}{2}a$, (since all are in equal probability to gain the first Game) which by the second Proposition is worth $\frac{1}{3}a$: Now since the second Gamester's Condition is as good, his Share is likewise $\frac{1}{3}a$, and so there remains to the third $\frac{1}{2}a$, whose Share might have been as easily found by itself.

PROP. IX. *In any number of Gamesters you please, amongst whom there are some fewer Games: To find what is any one's share in the Stake, we must consider what would be due to him, whose Share we investigate, if either he, or any of his Fellow-Gamesters should gain the next following Game; add all their*

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their Shares together, and divide the Sum by the number of the Gamesters, the Quotient is his Share you were seeking.

Suppose three Gamesters *A*, *B*, and *C*; *A* wants 1 Game, *B* 2, and *C* likewise 2, I would find what is the share of the Stake due to *B*, which I shall call $\frac{1}{3}q$.

First, we must consider what would fall to *B*'s Share, if either he, *A*, or *C*, wins the next Game; if *A* wins, the Game is ended, so he gets nothing; if *B* himself gain, then he wants 1 Game, *A* 1, and *C* 2; therefore, by the former Proposition, there is due to him in that Case $\frac{1}{3}q$, then if *C* gains the next Play, then *A* and *C* would want but 1, and *B* 2; and therefore, by the eighth Proposition, his Share would be worth $\frac{1}{2}q$; add together what is due to *B* in all these three Cases, viz. $0 + \frac{1}{3}q + \frac{1}{2}q$, the Sum is $\frac{5}{6}q$, which being divided by 3, the number of Gamesters, gives $\frac{5}{18}q$, which is the Share of *B* sought for: The Demonstration of this is clear from the second Proposition, because *B* has an equal hazard to gain $\frac{1}{3}q$ or $\frac{1}{2}q$, that is $\frac{0 + \frac{1}{3}q + \frac{1}{2}q}{3}$, i. e. $\frac{5}{18}q$: Now it's evident the Divisor 3 is the number of the Gamesters.

To find what is due to one in any Case; viz. if either he, or any of his Fellow Gamesters win the following Game; we must consider first the more simple Cases, and by their help the following; for as this Case could not be solved before the Case of the eighth Proposition was calculated, in which, the Games wanting were 1, 1, 2; so the Case, where the Games wanting are 1, 2, 3, cannot be calculated, without the Calculation of the Case, where the Games wanting are 1, 2, 2, (which we have just now perform'd) and likewise of the Case, where the Game

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Games wanting are 1, 2, 2, (which we have just now perform'd) and likewise of the Cafe, where the Games wanting are 1, 1, 3, which can be done by the eighth : And by this means you may reckon all the Cafes comprehended in the following Table and an infinite number of others.

| | | | | |
|---------------|---------|----------|-----------|----------|
| Games wanting | 1, 1, 2 | 1, 2, 2 | 1, 1, 3 | 1, 2, 3 |
| Their Shares | 4, 4, 1 | 17, 5, 5 | 13, 13, 1 | 19, 6, 2 |
| | 9 | 27 | 27 | 27 |

| | | | | |
|-------------|-----------|-------------|------------|----------|
| Games want. | 1, 1, 4 | 1, 1, 5 | 1, 2, 4 | 1, 2, |
| Shares | 40, 40, 1 | 121, 121, 1 | 178, 58, 7 | 542, 179 |
| | 81 | 243 | 243 | 729 |

| | | | |
|---------------|----------|-------------|-------------|
| Games wanting | 1, 3, 3 | 1, 3, 4 | 1, 3, 5 |
| Their Shares | 65, 8, 8 | 616, 82, 31 | 629, 87, 13 |
| | 81 | 729 | 729 |

| | | | |
|--------------|------------|--------------|--------------|
| Games want. | 2, 2, 3 | 2, 2, 4 | 2, 2, 5 |
| Their Shares | 34, 34, 13 | 338, 338, 53 | 353, 353, 23 |
| | 81 | 729 | 729 |

| | | | |
|--------------|------------|--------------|---------------|
| Games want. | 2, 3, 3 | 2, 3, 4 | 2, 3, 5 |
| Their Shares | 33, 55, 55 | 451, 195, 83 | 433, 635, 119 |
| | 243 | 729 | 1187 |

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As for the *Dice*; these Questions may be proposed, at how many Throws one may wager to throw 6, any Number below that, with one Die ; How many Throws are required for 12 upon two Dice ; or 18 on 3 ; and several other Questions to this purpose.

For the resolving of which, it must be consider'd, that in one Die there are six different Throws, all equally probable to come up ; for I suppose the Die has the exact figure of a Cube : On two Dice there are 36 different throws ; for in respect to every throw of one Die, any one throw of the 6 of the other Die may come up ; and 6 times 6 make 36. In three Dice there are 216 different throws ; for in relation to any of the 36 throws of two Dice, any one of the six of the third may come up ; and 6 times 36 make 216 : So in four Dice there are 6 times 216 throws, that is, 1296 : And so forward you may reckon the throws of any number of Dice, taking always, for the Addition of a new Die, 6 times the number of the preceding.

Besides, it must be observed, that in two Dice there is only one way 2 or 12 can come up ; two ways that 3 or 11 can come up ; for if I shall call the Dice A and B, to make 3 there may be 1 in A, and 2 in B, or 2 in A, and 1 in B ; so to make 11, there may be 5 in A, and 6 in B, or 6 in A, or 2 as well in A as B; for 10 there are likewise three Chances ; for 5 or 9 there are four Chances ; for 6 or 8 five Chances ; for 7 there are six Chances.

In 3 Dice there are
found for

| | |
|----------|----|
| 3 or 18 | I |
| 4 or 17 | 3 |
| 5 or 16 | 6 |
| 6 or 15 | 10 |
| 7 or 14 | 15 |
| 8 or 13 | 21 |
| 9 or 12 | 25 |
| 10 or 11 | 27 |

Prop. X. *To find at how many times one may undertake to throw 6 with one Die.*

If any should undertake to throw 6 the first time, it's evident there's one Chance gives him the Stake, and five which give him nothing ; for there are 5 throws against him, and only one for him. Let the Stake be called a , then he has one Expectation to gain a , and five to gain nothing, which, by the third Proposition, is worth $\frac{1}{6}a$, and there remains for the other $\frac{5}{6}a$; so he who undertakes, with one Die, to throw 6 the first time, ought to wager only 1 to 5.

2. Suppose one undertake, at two Throws of 1 Die, to throw 6, his Hazard is calculated thus ; if he throw 6 at the first, he has a the Stake ; if he do not, there remains to him one throw, which, by the former Case, is worth $\frac{1}{6}a$; but there is but one Chance which gives him 6 at the fist throw, and five Chances against him ; so there is one Chance which gives him a , and five which give $\frac{1}{6}a$, which by the second Proposition, is worth $\frac{5}{36}a$, so there remains to his Fellow-Gamester $\frac{25}{36}a$; so the Value of my Expectation to his, is as 11 to 25, i. e. less than 1 to 2.

By the same Method of Calculation, you will find, that his hazard who undertakes to throw 6 at three

three times with one Die, is $\frac{2}{5}a$; so that he can only lay 91 against 125, which is something less than 3 to 4.

He who undertakes to do it at four times, his hazard is $\frac{6}{125}a$, so he may wager 671 against 625, that is, something more than 1 to 1.

He who undertakes to do it at five times, his hazard is $\frac{4}{729}a$, so he can wager 671 against 625, that is, something less than 3 to 2.

His hazard who undertakes to do it at 6 times, is $\frac{11}{1681}a$, and he can wager 4651 against 3125, that is, something less than 2 to 1.

Thus any number of throws may be easily found; but the following Proposition will shew you a more compendious way of Calculation.

Prop. XI. *To find at how many times one may undertake to throw 12 with two Dice.*

If one should undertake it at one throw, it's clear he has but one Chance to get the Stake $\frac{2}{3}$ and 35 to get nothing; which, by the third Proposition, is worth $\frac{1}{36}a$.

He who undertakes to do it at twice, if he throw 12 the first time, gains a ; if otherwise, then there remains to him one throw, which, by the former Case, is worth $\frac{1}{36}a$; but there is but one Chance which gives 12 at the first throw, and 35 Chances against him; so he has 1 Chance for a , and 35 for $\frac{1}{36}a$, which by the third Proposition is worth $\frac{17}{1296}a$, and there remains to his Fellow-Gamester $\frac{112}{1296}a$.

From these it's easy to find the Value of his hazard, who undertakes it at four times, passing by his case who undertakes it at three times.

If he who undertakes to do it at four times throws 12 the first or second Cast, then he has a ; if not, there remains two other throws, which, by the former

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former Case, are worth $\frac{1}{125}a$; but for the same season, in his two first throws, he has 71 Chances which give him a , against 1225 Chances, in which it may happen otherwise; therefore at first he has 71 Chances which give him a , and 1225 which give him $\frac{1}{125}a$, which by the third Proposition is worth $\frac{14891}{15625}a$, which shews that their hazards to one another are as 178091 to 1500625.

From which Cases, it is easy to find the Value of his Expectation, who undertakes to do it at 8 times, and from that, his Case who undertakes to do it at 16 times; and from his Case who undertakes to do it at 8 times, and his likewise who undertakes to do it at 16 times; it is easy to determine his Expectation who undertakes to do it at 24 times: In which Operation, because that which is principally sought, is the number of throws, which makes the hazard equal on both sides, viz. to him who undertakes, and he who offers, you may, without any sensible Error, from the Numbers (which else would grow very great) cut off some of the last Figures. And so I find, that he who undertakes to throw 12 with two Dice, at 24 times, has some loss; and he who undertakes it at 25 times, has some advantage.

Prop. XII. *To find how many Dice one can undertake to throw two Sixes at the first Cast.*

THIS is as much, as if one would know, at how many throws of one Die, he may undertake to throw twice six: now if any should undertake it at two throws, by what we have shewn before, his hazard would be $\frac{1}{36}a$; he who would undertake to do it at 3 times, if his first throw were not 6, then there would remain two throws, each of which must be 6, which (as we have said) is worth $\frac{1}{36}a$; but if the first throw be 6, he want out

only one 6 in the two following throws, which by the tenth Proposition, is worth $\frac{1}{3}a$: but since he has but one Chance to get 6 the first throw, and five to miss it; he has therefore, at first, one Chance for $\frac{1}{6}a$, and five Chances for $\frac{1}{6}a$, which, by the third Proposition, is worth $\frac{5}{18}a$, or $\frac{2}{9}a$; after this manner still assuming 1 Chance more, you will find that you may undertake to throw two Sixes at 10 throws of one Die, or 1 throw of ten Dice, and that with some advantage.

Prop. XIII. *If I am to play with another one Throw, on this condition, that if 7 comes up I gain, if 10 be gains; if it happens that we must divide the Stake, and not play, to find how much belongs to me, and how much to him.*

Because of the 36 different Throws of the two Dice, there are six which give 7 and 3 which give 10, and 27 which equals the Game, in which case there is due to each of us $\frac{1}{4}a$: But if none of the 27 should happen, I have 6, by which I may gain a , and 3, by which I may get nothing, which by the third Proposition, is worth $\frac{1}{3}a$; so I have 27 Chances for $\frac{1}{4}a$, and 9 for $\frac{1}{3}a$, which by the third Proposition, is worth $\frac{9}{12}a$, and there remains to my Fellow-Gamester $\frac{3}{4}a$.

Prop. XIV. *If I were playing with another by turns, with two Dice, on this Condition, that if I throw 7 I gain, and if he throw 6 he gains allowing him the first Throw: To find the proportion of my Hazard to his.*

Suppose I call the Value of my Hazard x , and the Stakes a , then his Hazard will be $a-x$: When whenever it's his turn to throw, my Hazard is $\frac{x}{12}$.

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but when it's mine, the Value of my Hazard is greater. Suppose I then call it y ; now because of the 36 throws of two Dice, there are five which give my Fellow-Gamester 6, thirty-one which bring it again to my turn to throw, I have five Chances for nothing, and thirty-one for y , which, by the third Proposition, is worth $\frac{5}{36}y$; but I suppos'd at first my Hazard to be x ; therefore $\frac{5}{36}x = \frac{5}{36}y$, and consequently $y = \frac{5}{36}x$. I suppos'd likewise, when it was my turn to throw, the Value of my Hazard was y ; but then I have six Chances, which give me 7, and consequently the Stake, and thirty which give my Fellow the Dice, that is make my Hazard worth x : so I have six Chances for a , and thirty for x , which, by Prop. 3. is worth $\frac{6a+30x}{36}$, but this by supposition is equal to y , which is equal (by what has been prov'd already) to $\frac{36}{31}x$; therefore $\frac{30x+6a}{36} = \frac{36}{31}x$, and consequently $x = \frac{3}{31}a$, the Value of my Hazard, and that of my Fellow-Gamester is $\frac{5}{31}a$, so that mine is to his as 31 to 30.

Here follow some Questions which serve to exercise the former Rules.

1. *A* and *B* play together with two Dice, *A* wins if he throws 6, and *B* if he throws 7; *A* at first gets one throw, then *B* two, then *A* two, and so on by turns, till one of them wins. I require the proportion of *A*'s Hazard to *B*'s? *Answer*, It is 10355 to 12276.

2. Three Gamesters, *A*, *B*, and *C*, take 1 Counters, of which there are four white and blk

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black; the Law of the Game is this, that he shall win, who, hood-wink'd, shall first chuse a white Counter; and that *A* shall have the first choice, *B* the second, and *C* the third, and so, by turns, till one of them win. *Quær.* What is the proportion of their Hazards?

3. *A* wagers with *B*, that of 40 Cards, that is, 10 of every Suit, he will pick out four, so that there shall be one of every suit. *A*'s Hazard to *B*'s in this case is as 1000 to 8139.

4. Supposing, as before, 4 white Counters and 8 black, *A* wagers with *B*, that out of them he shall pick 7 Counters, of which there are 3 white. I require the proportion of *A*'s Hazard to *B*'s?

5. *A* and *B* taking 12 Counters, each play with three Dice after this manner; that if 11 comes up, *A* shall give one Counter to *B*; but if 14 comes up, *B* shall give one to *A*, and that he shall gain who first has all the Counters. *A*'s Hazard to *B*'s is 244140625 to 282429536481.

The Calculus of the preceding Problema is left out by Mons^r. Huygens, on purpose that the ingenious Reader may have the satisfaction of applying the former Method himself; it is in most of them more laborious than difficult: For Example, I have pitch'd upon the second and third, because the rest can be solv'd after the same Method.

PROBLEM I.

The first Problem is solv'd by the Method of Prop. 14. only with this difference, that after you have found the Share due to *B*, if *A* were to get no first

D

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first throw, you must subtract from it $\frac{1}{16}$ of the Stake which is due to *A* for his Hazard of throwing six at the first throw:

PROBLEM 2.

As for the second Problem, it is solv'd thus; Suppose *A*'s Hazard, when it is his own turn to chuse, be x ; when it is *B*'s; be y ; and when it is *C*'s, be z ; it is evident, when out of 12 Counters, of which there are 4 white, and 8 black, he endeavours to chuse a white one, he has four Chances to get it, and eight to miss it; that is, he has four Chances to get the Stake a , and eight to make his hazard wdrth y : so $x = \frac{4a + 8y}{12}$, and consequently $y = \frac{12x - 4a}{8}$. When it is *B*'s turn to chuse, then he has four Chances for nothing, and eight for x , (that is, to bring it to *C*'s turn) consequently $y = \frac{12x - 4a}{8}$; this Equation reduc'd gives $z = \frac{9x - 3a}{4}$ when it comes to *C*'s turn to chuse, then *A* has four Chances for nothing, and eight for x , consequently $x = \frac{1}{4}x$, therefore $\frac{1}{4}x = \frac{9x - 3a}{4}$ this equation reduc'd gives $x = \frac{3a}{8}$, and consequently there remains to *B* and *C* $\frac{15a}{8}$, which must be shar'd after the same manner, that is, so that *B* have the first Choice, *C* the next, and so on, till one of them gain; the Reason is; because it had been just in *A* to have demanded $\frac{1}{8}$ of the Stake for not playing, and then the Seniority fell to *B*; now $\frac{15a}{8}$, parted betwixt *B* and *C*, by the former Method, gives $\frac{3}{5}$ to *B*, and $\frac{2}{5}$ to *C*; so *A*, *B*, and *C*'s Hazards from the beginning were as 9, 6,

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I have suppos'd here the Senie of the Problem to be, that when any one chus'd a Counter, he did not diminish their number; but if he mis's'd of a white one, put it in again, and left an equal hazaad to him who had the following choice; for if it be otherwise suppos'd, A's share will be $\frac{25}{49}$, which is less than $\frac{1}{2}$.

Prob. 2. It is evident, that wagering to pick out 4 Cards out of 40, so that there be one of every Suit, is no more than wagering, out of 39 Cards to take three proposed Suits; for it is all one which Card you draw first, all the hazard being whether out of the 39 remaining you take 3, of which none shall be of the Suit you first drew: Suppose then you had gone right for three times, and were to draw your last Card, it is clear that there are 27 Cards, (*viz.* of the Suits you have drawn before) of which, if you draw any you lose, and 10, of which if you draw any, you have the Stake a ; so you have 10 Chances for a , and 27 for nothing, which by Prop. 3. is worth $\frac{10}{37}a$. Suppose again you had gone right only for two Draughts, then you have 18 Cards (of the Suits you have drawn before) which make you lose, and 20, which put you in the Case suppos'd formerly, *viz.* where you have but one Card to draw which, as we have already calculated, is worth $\frac{10}{37}a$; so you have 18 Chances for nothing, and 20 for $\frac{10}{37}a$, which, by Prop. 3. is worth $\frac{10}{37}a$. Suppose again you have 3 Cards to draw, then you have 9 (of the Suit you drew first) which make you lose, and 30 which put you in the case suppos'd last; so you have 9 Chances for nothing, and 30 for $\frac{10}{37}a$, which by Propos. 3. is worth $\frac{9}{37}a$, or $\frac{10}{37}a$, and you leave to your Fellow-Gamester $\frac{28}{37}a$; so your Hazard is to his as 1000 to 8139.

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It is easy to apply this Method to the Games that are in use amongst us : for Example, If *A* and *B*, playing at *Back-gammon*, *A* had already gain'd one end of three, and *B* none, and if *A* had the Dice in his Hand for the last throw of the second end all, his Men but two upon the Ace Point being already cast off : *Quær*. What is the proportion of *A*'s Hazard to *B*'s ?

Solution : There being of the 36 Throws of two Dice, six which give Doublets ; if *A* throw any of the six, he has the stake a ; if he throw any of the other thirty, then he wants but one Game, and his Fellow-Gamester three, which by Prop. V. is $\frac{1}{4}a$; so *A* has six Chances for a , and thirty for $\frac{1}{4}a$, which, by Prop. III. is worth $\frac{12}{144}a$, and there remains to his Play-Fellow $\frac{12}{144}a$; so *A*'s Hazard to *B*'s is as 129 to 15, that is, less than 9 to 1.

Supposing the same Case, and if their Bargain had been, that he gain'd three ends before the other gain'd one, should have double of what each stak'd, that is, the Stake and a half more, then there had been due to *A* $\frac{282}{288}$ of the Stake, that is, *B* ought only to take $\frac{1}{12}$, and leave the rest to *A*.

Thus likewise, if you apply the former Rule to the *Royal-Oak Lottery*, you will find, that he who wagers that any Figure shall come up at the first throw, ought to wager 1 against 31 ; that he who wagers it shall come up at one of the two throws, ought to wager 63 against 961 ; that he who wagers that a Figure shall come up at once in three times, ought to lay 125055 against 923521, &c. it being only somewhat tedious to calculate the rest. Where you will find, that the equality will not find, that the equality will not fall as some imagine on 16 Throws, no more than the equality of wagering at how many Throws of one Die 6 shall come up,

falls on three ; the contrary of which you have seen already demonstrated : You will find by calculation, that he has the Disadvantage, who wagers, that **i** of the 32 different Throws of the *Royal-Oak Lottery* shall come at once of 20 times, and that he has some advantage, who wagers on 22 times, so the nearest to Equality is on 21 times. But it must be remembred, that I have suppos'd in the former Calculation, the Ball in the *Royal-Oak Lottery*, to be regular, tho' it can never be exactly so ; for he, who has the smallest Skill in Geometry, knows that there can be no regular Body of 32 sides ; and yet this can be of no Advantage to him who keeps it.

To find the Value of the Throws of Dice, as to the Quantity.

NOthing is more easy, than by the former Method to determine the Value of any number of Throws of any number of Dice ; for in one throw of a Die, I have an equal Chance for 1, 2, 3, 4, 5, 6, consequently my Hazard is worth their Sum 21 divided by their Number 6, that is, $3\frac{1}{2}$. Now if one throw of a Die be worth $3\frac{1}{2}$, then two throws of a Die, or one throw of two Dice is worth 7, two throws of two Dice, or one throw of four Dice is worth 14, &c. The general Rule being to multiply the Number of Dice, the Number of Throws, and $3\frac{1}{2}$ continually.

This is not to be understood as if it were an equal Wager to throw 7, or above it, with two Dice at one throw ; for he who undertakes to do so, has the Advantage by 21 against 15. The meaning is only, if I were to have a Guinea, a Shilling, or anything else, for every Point that I threw with two Dice at one throw, my Hazard is worth 7 of these, because he who gave me 7 for it, would have an equal probability.

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bility of gaining or losing by it, the Chances of the Throws above 7, being as many as of these below it : So it is more than an equal Wager to throw 12 at least at two Throws of two Dice, because it is more probable that 14 will come, than any one Number besides, and as probable that it will be above it as below it ; but if one were to buy this Hazard at the rate abovemention'd, he ought just to give 14 for it. The equal wager in one Throw of two Dice, is to throw 7 at least one time, and 8 at least another time, and so *per vices* : The Reason is, because in the first Case I have 21 Chances against 15, and in the second 15 Chances against 21.

Of RAFFLING.

IN Raffling, the different Throws and their Chances are these ; Where it is to be observed, that of the 216 different Throws of three Dice, there are only 96 that give Doublets, or two, at least, of a kind ; so it is 4 to 5 that with three Dice you shall throw Doublets, and it is 1 to 35 that you throw a Raffle, or all three of a Kind. It is evident likewise, that it is an even Wager to throw 11 or above it, because there are as many Chances for 11, and the Throws above it, as for the Throws below it ; but tho' it be an even Wager to throw 11 at one Throw, it is a Disadvantage to wager to throw 22 at two Throws, and far more to wager to throw 33 at three Throws ; and yet it is more than an equal Wager that you shall throw 21 at two Throws in Raffling, because it is as probable that you will, as that you will not throw 11, at least, the first time, and more than probable that you will throw 10, at least the Second Time.

| Throws. | Chanc. |
|---------|--------|
| 3 | 18 |
| 4 | 17 |
| 5 | 16 |
| 6 | 15 |
| 7 | 14 |
| 8 | 13 |
| 9 | 12 |
| 10 | 11 |

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For an instance of the plainness of the preceding Method, I will shew, how by simple Subtraction, the most part of the former Problems may be solv'd.

Suppose *A* and *B*, playing together, each, of them stakes 32 Shillings, and that *A* wants one Game of the number agreed on, and *B* wants two; to find the share of the Stakes due to each of them. It's plain, if *A* wins the next Game, he has the whole 64 Shillings; if *B* wins it, then their Shares are equal; therefore says *A* to *B*, If you will break off the Game, give me 32, which I am sure of, whether I win or lose the next Game; and since you will not venture for the other 32, let us part them equally, that is, give me 16, which with the former 32 make 48, leaving 16 to you.

Suppose *A* wanted one Game, and *B* three; if *A* wins the next Game, he has the 64 Shillings; if *B* wins it, then they are in the condition formerly suppos'd, in which case there is 48 due to *A*; therefore says *A* to *B*, give me the 48 which I am sure of, whether I win or lose the next Game; and since you will not hazard for the other 16, let us part them equally; that is, give me 8, which, with the former 48, make 56, leaving 8 to you; and so all the other Games may be solv'd after the same manner.

Suppose *A* wagers with *B*, that with one Die he shall throw 6 at one of three Throws, and that each of them stakes 108, Guineas; to find what is the proportion of their Hazards. Now there being in one Throw of a Die but one Chance for 6, and five Chances against it, one Throw for 6 is worth $\frac{1}{6}$ of the Stake; therefore says *B* to *A*, of the 216 Guineas take a sixth part for your first Throw, that is, 36; for your next Throw take a sixth part of the remaining 180, that is, 30; and for your third Throw, take a sixth part of the remaining 150, that is, 25, which

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which in all make 91, leaving to me 125; so his hazard who undertakes to throw 6 at one of the three Trows, is 91 to 125.

Suppose *A* had undertaken to throw 6 with one Die at one Throw of four, and that the whole Stake is 1296; says *A* to *B*, every Throw for 6 of one Die, is worth the sixth part of what I throw for; therefore for my first Throw give me 216, which is the sixth part of 1296, and there remains 1080, I must have the sixth part of that, viz. 180, for my second Throw; and the sixth part of the remaining 900, which is 150, for my third Throw; and the sixth part of the last remainder 750, which is 125 for my fourth; all this added together makes 671, and there remains to you 625; so it is evident, that *A*'s Hazard, in this Case, is to *B*'s 671 to 525.

Suppose *A* is to win the Stakes (which we shall suppose to be 36 (if he throws 7 at once or twice) with two Dice, and *B* is to have them if he does not; says *B* to *A*, the Chances which give 7 are 6 of the 36, which is as much as 1 of 6; therefore for your first Throw you shall have a sixth part of the 36, which is 6; and for your next Throw a sixth part of the remainder 30, which is 5; this in all makes 11; so you leave 25 to me; so *A*'s Hazard is to *B*'s as 11 to 25.

It were easy, at this rate, to calculate the most intricate Hazards, were it not that Fractions will occur; which, if they be more than $\frac{1}{2}$, may be supposed equal to an Unit, without causing any remarkable Error in great Numbers.

It will not be amiss, before I conclude, to give you a Rule for finding in any number of Games the Value of the first, because Huggens's Method, in that Case, is something tedious.

Suppo

Suppose *A* and *B* had agreed, that he should have the Stakes who did win the first 9 Games, and *A* had already won one of the 9; I would know what share of *B*'s Money is due to *A* for the Advantage of this Game. To find this, take the first eight even Numbers 2, 4, 6, 8, 10, 12, 14, 16, and multiply them continually, that is, the first by the second, the product by the third, &c. take the first eight odd Numbers 1, 3, 5, 7, 9, 11, 13, 15, and do just so by them, the product of the even Number is the Denominator, and the product of the odd Number the Numerator, of a Fraction, which expresseth the quantity of *B*'s Money due to *A* upon the winning of the first Game, of 9; that is, if each stak'd a number of Guineas, or Shillings, &c. express'd by the Product of the even Numbers, there would belong to *A*, of *B*'s Money, the Number express'd by the product of the odd Numbers. For Example, Suppose *A* had gain'd one Game of 4, then by this Rule, I take the three first even Numbers, 2, 4, 6, and multiply them continually, which make 48, and the first three odd Numbers, 1, 3, 5, and multiply them continually, which make 15; so there belongs to *A* $\frac{1}{4}$ of *B*'s Money, that is, if each stak'd 48, there would belong to *A*, besides his own, 15 of *B*'s. Now by *Huygens*'s Method, if *A* wants but three Games while *B* wants four, there is due to *A* $\frac{3}{4}$ of the Stake; by this Rule there is due to *A* $\frac{3}{4}$ of *B*'s Money, which is $\frac{3}{8}$ of the Stake, which, with his own $\frac{3}{8}$ of the Stake, makes $\frac{3}{4}$ or $\frac{3}{2}$ of the Stake; and so in every Case you will find *Huygens*'s Method, and this will give you the same Number: A Demonstration of it you may see in a Letter of Monsieur *Pascal*'s to Monsieur *Fermat*; though it be otherwise express'd there than here, yet the consequence is easily supply'd. To prevent

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prevent the labour of Calculation, I have subjoin'd the following Table, which is calculated for two Gamblers, as Monsieur Huygens's is for three.

If each of us stake 256 Guineas in

| | 6 | 5 | 4 | 3 | 2 | 1 |
|---------------------------------------|-----|-----|-----|-----|-----|-----|
| 1 st Game | 63 | 70 | 80 | 96 | 128 | 256 |
| 2 nd 1 st Games | 126 | 140 | 160 | 192 | 256 | |
| 3 rd 1 st Games | 182 | 200 | 224 | 256 | | |
| 4 th 1 st Games | 224 | 240 | 256 | | | |
| 5 th 1 st Games | 248 | 256 | | | | |
| 6 th 1 st Games | 256 | | | | | |

These belongs to me 256 of my Play-fellow

The Use of the Table is plain; for let our Stakes be what they will; I can find the Portion due to me upon the winning the first, or the first two Games, &c. of 2, 3, 4, 5, 6. For Example, If each of us had stak'd 4 Guineas, and the number of Games to be play'd were 3, of which I had gain'd 1, I say, As 256 is to 96, so is 4 to a fourth part. And if one of us had stak'd 256 Guineas, and the other 256, leaving

256 : 96 :: 4 : 1. is to say that

To find what is the Value of his Hazard, who undertakes, at the first Throw, to cast Doublets, in any given number of Dice.

In two Dice it is plain, to avoid Doublets, every one of the six different Throws of the first, can only be combin'd with five of the second, because one of the six is of the same kind, and consequently makes Doublets; for the same Reason, the thirty Throws of two Dice, which are not Doublets, can only be combin'd with four Throws of a Dice; so generally it is this Series,

$$\frac{6 \times 5 \times 4 \times 3 \times 2 \times 1 \times 0}{6 \times 6 \times 6 \times 6 \times 6 \times 6}, &c.$$

The second Series is the Sum of the Chances, and the first the Number of Chances against him who undertakes to throw Doublets, each Series must be continu'd so many terms, as are the Number of Dice. For Example, If one should undertake to throw Doublets at the first Throw of four Dice, his Adversary's Hazard is $\frac{6 \times 5 \times 4 \times 3 \times 2}{6 \times 6 \times 6 \times 6} = \frac{360}{1296}$ or $\frac{5}{18}$ leaving to him $\frac{13}{18}$, so he has 13 to 5. In four Dice, you see the Chances against him are 0, because then there must necessarily be Doublets to own.

Of WHIST.

If there be four plodying at Whist, it is 15 to 1 that any two of them shall not have the four Honours, which I demonstrate thus.

Suppose the four Gamester's be A, B, C, D: If A and B had, while the Cards are a dealing already

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ready got three Honours, and wanted only one, since it is as probable that *G* and *D* will have the next Honour, as *A* and *B*; if *A* and *B* had laid a Wager to have it, there is due to them but $\frac{1}{4}$ of the Stake: If *A* and *B* wanted two of the four, and had wager'd to have both those two, then they have an equal hazard to get nothing, if they miss the first of these two, or to put themselves in the former Case if they get; so they have an equal Hazard to get nothing, or $\frac{1}{2}$, which by Prop. 1. is worth $\frac{1}{4}$ of the Stake; so if they want three Honours, you will find due to them $\frac{1}{2}$ of the Stake; and if they wanted four, $\frac{15}{16}$ of the Stake leaving *C* and *D* $\frac{1}{16}$; so *C* and *D* can wager 15 to 1, that *A* and *B* shall not have all the four Honours.

It is 11 to 5 that A and B shall not have three of the four Honours, which I prove thus :

1. It is an even Wager, if there were but three Honours, that *A* and *B* shall have two of these three; since 'tis as probable that they will have two of the three, as that *C* and *D* shall have them; consequently, if *A* and *B* had laid a Wager to have two of three, there is due to them $\frac{1}{2}$ of the Stake. Now suppose *A* and *B* had wager'd to have three of four, they have an equal hazard to get the first of the four, or miss it; if they get it, then they want two of the three, and consequently there is due to them $\frac{1}{2}$ of the Stake; if they miss it, then they want three of the three; and consequently there is due to them $\frac{1}{2}$ of the Stake; therefore, by Prop. 2. their Hazard is worth $\frac{15}{16}$, leaving to *C* and *D* $\frac{1}{16}$.

II : *On the Hazard of having two of three Honours, when the Stake is 15 to 1.*

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A and B playing at Whist against C and D; A and B have eight of ten, and C and D nine, and therefore can't reckon Honours; to find the proportion of their Hazards.

There is $\frac{3}{8}$ due to A and B upon their hazard of having three of four Honours, but since C and D want but one Game, and A and B two, there is due to A and B but $\frac{1}{2}$, or $\frac{4}{8}$ more upon that Account, by Prop. 4, this in all makes $\frac{7}{8}$, leaving to C, and D $\frac{1}{8}$; so the hazard of A and B to that of C and D, is as 9 to 7.

In the former Calculations I have abstracted from the small difference of having the Deal and being Seniors.

All the former Cases can be calculated by the Theorems laid down by Monsieur Huygens; but Cases more compos'd require other Principles: For the easy and ready Computation of which, I shall add one Theorem more, demonstrated after Monsieur Huygens's Method.

THEOREM.

If I have p Chances for a , q Chances for b , and r Chances for c , then my hazard is worth $\frac{ab+bc+ac}{p+q+r}$; that is, a multiplied into the number of its Chances, added to b , multiplied into the number of its Chances, added to c , multiplied into the number of its Chances, and the Sum divided by the Sum of Chances of a, b, c .

To investigate as well as demonstrate this Theorem, suppose the value of my hazard be x , then x must be such, as having it, I am able to purchase as good a Hazard again in a just and equal Game. Suppose the Law of it be this, That playing with so many Gamesters as, with myself, make up the number $p+q+r$, with as many of them as the number x pre-

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presents, I make this bargain, that whoever of the ~~win~~ shall give me a , and that I shall do so to the ~~win~~ ; with the Gamesters represented by a number of q , I bargain to get b , if any of the win, and to give b to each of them, if I win it self; and with the rest of the Gamesters, whose number is $r-1$, I bargain to give, or to get c af the same manner : Now all being in an equal probability to gain, I have p Chances to get a , Chances to get b ; and $r-1$ Chances to get c , a one Chance, viz. when I win myself, to get $px+rx-ap-bq-rc+c$, which if it be suppos'd equ to c , then I have p Chances for a , q Chances for b , and r Chances for c (for I had just now $r-1$ Chanc for it) and therefore, in Case $px+qx+rx-ap-
rx+c=c$, then is $x=\frac{ap+bq+cr}{p+q+r}$.

By the same Way of reaforming you will find, if have p Chances for a , q Chances for b , r Chanc for c , and s Chances for d , and that my Hazard $\frac{ap+bq+cr+ds}{p+q+r+s}$, &c.

In NUMBERS.

If I had two Chances for 3 Shillings, so Chances for 5 Shillings, and one Chance for Shillings, then, by this Rule, my Hazard is worth 5 Shillings ; for $\frac{2 \times 3 + 4 \times 5 + 1 \times 9}{7} = 5$; and it easy to prove, that with 5 Shillings I can purcha a like Hazard again ; for suppose I play with six others, each of us staking 5 Shillings ; with two them I bargain, that if either of them win, he mu give me 3 Shillings, and that I shall do so to them and with the other four I bargain just so, to give ~~so~~^{the} 5 Shillings : This is a just Game, and all

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ing in an equal probability to win; by this means I have two Chances to get 3 Shillings, four Chances to get 5 Shillings, and one Chance to get 9 Shillings, &c. when I win myself; for then out of the Stake, which makes 35 Shillings, I must give the first two 6 Shillings; and the other four 20 Shillings, so there remains just 9 to myself.

It is easy, by the Help of this Theorem, to calculate in the Game of Dice, commonly call'd Hazard, what Main's are best to set on, and who has the Advantage, the Caster or Setter. The Scheme of the Game, as I take it, is thus:

| Throws next following for | | |
|---------------------------|-------------|-------------------|
| Main. | The Caster. | The Setter. |
| V. | V. | II. III. XI. XII. |
| VI. | VI. XII. | XI. II. III. |
| VII. | VII. XI. | XII. II. III. |
| VIII. | VIII. XII. | XI. II. III. |
| IX. | IX. | II. III. XI. XII. |

By an easy Calculation you will find, if the Caster has IV, and the Setter VII, there is due to the Caster $\frac{1}{3}$ of the Stake; if he has V, $\frac{1}{2}$ of the Stake.

V against VII, $\frac{1}{3}$ of the Stake.

VI against VII, $\frac{1}{2}$ of the Stake.

IV against VI, $\frac{1}{3}$ of the Stake.

V against VI, $\frac{1}{2}$ of the Stake.

IV against V, $\frac{1}{3}$ of the Stake.

I need not tell the Reader, that IV is the same with X, V with IX, and VI with VIII.

Suppose then VII be the Main: To find the Proportion of the Hazard of the Caster to that of the Setter.

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By the Law of the Game, the Caster, b
throws next; has four Chances for nothi
these II, III, XII; eight Chances for thi
Stake, *viz.* those of VII, XI; six Chance
viz. those of IV, X; eight Chances for
those of V, IX; and ten Chances for ¹
those of VI, VIII; so his Hazard, by the p
Theorem, is

$$\frac{4 \times 0 + 8 \times 1 + 6 \times \frac{1}{2} + 8 \times \frac{2}{3} + 10 \times \frac{1}{4}}{36}$$

Now to save the Trouble of a tedious Re
suppose the Stake which they play for be
is, the Setter had laid down 18; in that Ca
ry one of these Fractions are so many Par
Unit, which being gather'd into one Sur
 $17\frac{1}{3}$ to the Caster, leaving $18\frac{2}{3}$ to the
so the Hazard of the Caster is to that of th
244,251.

Suppose VI, or VIII, be the Main, 1
Share of the Caster is

II.
III. VI. IV. V.
XI. XII. X. IX. VIII. VII.

$$5 \times 0 + 6 \times 1 + 1 \times 6\frac{1}{3} + 8 \times \frac{2}{3} + 5 \times \frac{1}{2} + 6 \times \frac{9}{11} =$$

leaving to the Setter $18\frac{16}{33}$; so the H
the Caster is to that of the Setter as if
7295.

Suppose V, or IX, be the Main, then t
of the Caster is

II.

III.

XI.

IV. VI.

XII. V. X. IX. VIII. VII.

$$6 \times 0 + 4 \times 1 + 6 \times \frac{1}{3} + 4 \times \frac{1}{2} + 10 \times \frac{1}{5} + 6 \times \frac{1}{3} = 17\frac{2}{3}$$

leaving to the Setter $\frac{86}{177}$; so the Hazard of the Caster is to that of the Setter as 1396 to 1439.

It is plain, that in every Case the Caster has the Disadvantage, and that V, or IX, are better Mains to set on that VII, because, in this last Cast, the Setter has but 18 and $\frac{1}{3}$, or $\frac{55}{3}$; whereas, when V or IX is the Main, he has $18\frac{86}{177}$; likewise VI, or VIII, are better Mains than V, or IX, because $\frac{19}{3}$ is a greater Fraction than $\frac{19}{5}$.

All those Problems suppose Chances, which are in an equal Probability to happen; if it should be supposed otherwise, there will arise Variety of Cases of a quite different Nature, which, perhaps, it were not unpleasant to consider: I shall add one Problem of that Kind, leaving the Solution to those who think it merits their Pains.

*In Parallelipipedo cuius latera sunt ad invicem in ratione a, b, c: Invenire quot*a* vice quicvis fuscipere potest, ut datum quodvis planum, v. g. a b jaciat.*



THE
LONGITUDE
EXAMIN'D.

A Short Epistle to the *Longitudinarians*.

Gentlemen,

TH E Books that are written about the Longitude, are so acceptable to the Publick, that the whole Edition is commonly sold off, before any of them can reach our Northern Booksellers; therefore I hope you will not refuse to admit me into your Number, tho' my Attempt is publish'd so late; neither will you look upon me as your Enemy, if I overthrow all your Schemes, to set up mine; for, if you'll believe me, I am in perfect Charity with you all: But Custom will prevail, and then I must shew what I can do in the Beginning of my Book, that my Readers may enter upon the Description of my Engine with a good Opinion of my Skill; tho' the main Reason is, that, without Animadversions upon the Attempts of others, I could not swell this to a Six-penny Book, unless I had embellish'd the Recommendation of my Device with fine Metaphors, and clever Comparisons; quoting the Scripture in one Place, and the Poets in another; or filling up Voids with Passages taken out of the Apostolical Constitutions. But I never had the Knack of speaking

Speaking much, when I had but little to say. I might, indeed, with the Printer's good Management, have made four Pages of the Commissioners Names in Capitals, and then have humbly submitted my Essay, and subscrib'd myself their devoted and obedient Servant in two Pages more; which, with the Copy of the Act of Parliament, and Title-Page, would have made up one Sheet: An Introduction of Astronomical, Geographical, and Mechanical Definitions, to shew that I was Somebody, might have fill'd the next Sheet; and the Devil is in't if I could not have made sixteen Pages of my Movement; and so, by the Help of FINIS and ERRATA, compleated my three Sheets. But then I consider'd, (since I am sure of being right) that it was my best Way to go to Sea first, and give the Mariners such Ocular Demonstration of my Contrivance, that I shall have a sufficient Number of Witnesses of my Success, to vouch the Account of which I shall, at my Return, lay before the Commissioners, and so carry off the twenty Thousand Pounds. As for the Introduction, I should have thought it very ill Manners, to begin my Book, as if I meant to teach First Principles to those Learned Philosophers by whom I am to stand or fall. If it be ask'd, why I wrote the Book at all, I'll frankly answer, That I wanted Money; and that if I had thought that the Commissioners would have been prevailed upon to have given me some, to carry on Experiments, I had never set Pen to Paper. For this very Reason, I shan't say a Word about my New Invention, till its proper Place. And if the Bookseller does not cut open the Sheets, whoever has a Mind to know what I drive at, must buy the Book: Peeping in, won't do; for I shan't begin a Paragraph with the Description of my Curiosities, or write the Names of any of my Machines in Italick Characters. All that

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I shall say here, is, That I have try'd all my Experiments at Land, with desir'd Success, and as soon as the Bookseller has paid me, I'll go to Sea; and if, after all, I fail in the Attempt, yet—Vobiscum certasse juvabit. I am, Gentlemen,

Your most devoted, most obedient,
and most humble Servant,

Jeremy Thacker, Philomath.

Well-wisher to the Twenty Thousand Pounds.

Advertisement concerning the Longitude.

“ **I** T is now well nigh towards half a Year, since
“ my good Genius, and my Self, found out
“ a Method for discovering LONGITUDE, which I
“ had publish'd before, had it not been on Account
“ of the Creatures of Trap and Discovery, who, (I
“ had Reason to fear) would have run away with
“ the Secret that Nature had confess'd to ME, and
“ had refus'd to THEM, as often as they have ask'd
“ her for it. But now, that Things are so settled,
“ that no Body can rob me of the Benefit of my
“ Invention, I publish this to defy all that can be
“ done by those of the Snearing and Grinning Kind,
“ in their proper Employment of Ridicule and Gri-
“ mace: And therefore I expect all my Readers to
“ be Merry or Angry, or Grave or Serious, upon
“ this Occasion; but I must (and indeed I dare)
“ submit myself to the Multitude, who, if I am
“ not mistaken, will declare me a Fool or Mad-
“ man, with Pomp and Ceremony, for being so po-
“ sitive; and therefore I do, by Astrological Cal-
“ culation, prognosticate, that some will *defire* I
“ should

" should be in the *Wrong*; others will have a *Suspicion* that I am in the *Right*; and the *Ignorant* will not know whether I am *Right or Wrong*.

Jeremy Thacker.

WHAT if the greatest Part of the Pack have run upon a false Scent, may not the hindmost Dog hit it off? Perhaps, from my comparing the *Seekers* after the *Longitude*, to a Pack of Hounds, some arch Wags will say, that if one or two Dogs run mad, it is ten to one but all the rest eatch the Infection, and so look upon him as a Mad-man; let 'em sneer on; for if I can but demonstrate myself to be in the *Right*, and all the rest in the *Wrong*, (as I am confident I can) their Laughing will be turn'd into Admiration; and when I receive the Reward, they'll say, *Who wou'd have thought it?*

If I should follow the Example of the greatest Part of the *Longitudinarians*, that wrote after the first Attempt, I should take Mr. *Whiston* and Mr. *Ditton* in Hand, shipwreck their *Hulls*, drown their *Sounds* in a Tempeft, lift up the Waves to intercept the Sight of their *Fires*, and break their *General Peace*; but Gratitude forbids: They sprung the Twenty Thousand Pounds, and I hope to get it, I ought to be civil to them. Then let Mr. *D.* rest assur'd, that I will neither meddle with his *Longitude*, nor his *New Law of Fluids*; and poor Mr. *W.* has been so often handled as a *Longitudinarian* and a *Latitudinarian*, so amaz'd at the Bursting of his *Mortar*, and one of his *Sbells*, and so frighten'd with the Fall of another *unlighted one*, that it would be as barbarous as ungrateful for me to insult over

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him. No, I shall always own him the Maker of my Fortune. I had no great Acquaintance, no Friends at Court; I could by no Means have procur'd an Act of Parliament for my Encouragement: My Engine was ready these three or four Years; so I was glad when he stirr'd. I lay still, well-knowing that he was beating the Bush for me to catch the Hare.

Before Mr. Hobbs thinks of sending his Spring-Movement to Sea, let him know how to make the Month of *June* in one Year, just as hot as the same Month in another, and so of every Day and Month in all Years; then his Instrument will be equally hasten'd and retarded at the same Seasons; and then he may polish his Pivots, and make an *Aëtherial Oil* that won't thicken and increase the Friction of his Watch.

Mr. Bill—y (after having acquainted us with several admirable and surprizing *Phænomena* of Nature, which he took for *Conjuring*, the first Time he saw them, but now dares venture to perform himself, (and by himself) very reasonably tells us That since the *Phosphorus*, *Glass-Devils* in Water &c. which would, to a Stranger, seem to be actuated by Magic; to us that are wiser, appear to be the Effects of no other Arts, but *Chymistry* and *Legerdemain*; his finding out the Longitude, after so many have attempted it in vain, is a Thing in stranger than it is true. His Movement is still behind the Curtain, but I'll think the best of it; and since he has vowuchsafed to tell us, *That he will, by Means of a long Pendulum, have a steady Motion in an irregular one*, I'll help them out, and assure him, that he will succeed, if he will do one Thing more, and that is, — prove Sir Isaac Newton's first *Law of Motion* to be false.

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I have little to say to Mr. Br—e, the Corrector of the Moon's Motion; but if his Application of it be practicable for trying to find the Longitude, I'll turn him over to the Astronomers, for the Examination of his Theory; and I would not be in his Case, if he should fall into the Hands of Dr. John Keil, who knows how to revenge the least Injury done to Dame Nature his Mistress, by the false Reports of bad Philosophers.

The Latitude, no doubt, may be exactly found by Signior Al—ri; but if he would discover the Longitude by his Machine, he should desire his Workmen to make him a long Leaver, not to move, but to stop the Earth; or if Ptolemy has done that for him already, let him shove up his Leaver, and stop the *Primum Mobile*: If he wants Help, Mr. K—th will lend him an Hand, and tell him what Star he shall chuse for an Eastern or a Western Pole. However, let not our Italian Gentleman be discourag'd from giving us the Figure of his Engine; for he is not the first Professor of Mathematics that has fallen short of the Longitude: And though I can't commend his Scheme, because I am his Rival in this Case, yet, if he'll try for the Philosopher's Stone, or *square the Circle*, I'll subscribe to it. And if my Friend K—th would have his Method effectual, let him take a Journey to the Moon, where he will be certain of his Longitude, by his Observations of the impending Earth; he may find a sufficient Number of *Ganza's* among the *Latitudinarians* to carry him thither, and the Lunatick Attraction between the *Moon* on the one Hand, and himself and the *Ganza's* on the other, will make his Voyage speedy.

Mr. J. H. Writer of the Essay, has such a fertile Brain at Invention, that I know not how to deal with him :

— *He'll raise Objections dark and nice,
And after solve 'em in a Trice.*

And if I demolish one of his Movements, he'll pop upon me in a Moment with another. If I tell him, that the Mercury in his portable Barometer with the spiral Bason, will vibrate ten or twenty Inches by the very Shake of the Ship, because the common portable one, which is ten or twenty times less sensible as to the Mercury's Rise and Fall, will, with the least Shake, vibrate half an Inch) he'll substitute Dr. Hook's Marine Barometer, and have me there again : But then (granting him his Theory of the Tides) he must consider that the Moon raises a Tide in the Atmosphere, as well as the Ocean ; and as he rises from his Level with his Barometer in hand, where he expects the Liquor to descend, he will find himself baulk'd, because the Height of the counterposing Atmosphere, will not decrease in that Case, as it would do at Land.

But then the *Pendulum* in the *Center of the Gravity of the Ship*, must it not always vibrate? That it will be in Motion all the while that the Ship goes, I readily grant; but then it must be in *absolute Motion*; for if ever the Ship goes steady it will be at *relative Rest*; (that is, (in mechanical English) at Rest in Respect of the Things about it in the Ship) and therefore it will not move his Watch-Work. If he would have this Instrument go, let him consult about it with the Inventors of a perpetual Motion; * and for his Time-keeper by a *Vacuum*, let him

* He may bear of several at Birmingham or Sheffield.

him ask Advice of that Metaphysical Gentleman who has wrote a Book to disprove the Existence of Matter.

I have seen no more Attempts for the Longitude, except Mr. W^a—n's Advertisement, wherein he promises a Clock to make the Longitude known to those of the meanest Capacity; therefore since I think myself none of the Vulgar, the Expectation of his Wheel-Work shan't delay my Book; let the Tars examine the Machine, and judge of it.

There is another Gentleman that has a great Volume coming out, for which he hopes to have the Twenty Thousand Pounds. His first Page of the Quarto sent before, (to tell the World that he is coming) he dedicates to the KING, his next to the PRINCE, the third to the Royal Society, and the fourth to the Reader: So far I read of him; for the Language look'd like English, and the Printer had shew'd himself a well bred Man in the Distances of the Lines, and Bigness of the Letters, whose Size he proportion'd to the Quality of the Patrons. The Body of the Book was wrote in a Language that I could not understand, and so I must suspend my Judgment, till I have sent it to be perus'd by my learned Friend Mr. Gr—n, of Cambridge; for this Book may contain some of the Conclusions which follow from the Principles of his new Philosophy.

In a Word, to put an End to all the Methods for discovering of the Longitude that have been publish'd hereafter, (always excepting my own) there are but two Ways by which it can be found, *viz.* *By the Improvement of Astronomy, or by the perfecting of Clock-Work.*

It is to be hop'd that Astronomy will soon be carry'd so far as to serve for this Purpose, unless the great Mr. L—, with an Industry equal to his Candour, should join the Fluxions and Series, which

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be invented, to his known Skill in the Laws of *Centripetal* and *Centrifugal Forces*, and so vouchsafe to perform the Work for the Benefit of Mankind.

But if Astronomy was much more improv'd, Telescopes of a competent Length, for Observations of such a Nicety as is requir'd in this Case, would not be manageable at Sea, even tho' the Observer should place himself in the Center of Gravity of the Ship, where there is the least Motion of all; besides in foul Weather, when the Longitude is most wanted, no Cœlestial Body would be seen, to make Observations.

What remains, is a *Time-Keeper*.

A long Pendulum-Clock measures Time better than any other Machine whatever, at Land; but it can by no Means be brought to do it at Sea with the same Exactness, for the following Reasons :

1. Because the Pendulum does not vibrate in a Cycloid.
2. Because the circular Arcs which it describes, are, by the Motion of the Ship, made to be unequal, and therefore not *Isochronal*, or perform'd in the same Time.

It is demonstrated by Mathematicians, that if a Pendulum (*Fig. 1.*) swings in a *Cycloid*, as APB, all its Swings or Vibrations, whether great, as APB, or small, as DP π , are perform'd in the same Time; but the Pendulum P being fasten'd to the Center T of the *Semi-circle* FPG by the Thread or Wire TP, tends to swing in the *Semi-circle* FPG, in which unequal Arcs are not gone thro' in the same Time by the Pendulum. Some Clock-makers indeed have us'd *Cycloidal Cheeks*, as AT and TB, to guide the Thread or Rod of the Pendulum; but the great Friction between the Cheeks at T, and again

gainst 'em along A T and T B, has made the Remedy worse than the Disease ; and therefore Pendulums have again been made to swing in Circles ; but the Thread or Rod of the Pendulum, being made pretty long, and vibrating only short Arcs of a large Circle, the Swings are Isochronal, because the small Arcs of a Cycloid; and the small Arcs of a large Circle coincide. As for Example, if the Semi-circle FPB be of about nine Inches Radius, and the Pendulum describes nearly a Quadrant of it each Vibration, as it will do in going from *a* to *b*, then the Arc describ'd, will run pretty much out of the Cycloid ; but if the Radius of FPD, or what is the same, the Rod of the Pendulum, be four times as long as that which is made use of to swing Seconds, and the Pendulum itself pretty heavy, it will swing in the Arc DP π , where the Circle and the Cycloid are sensibly the same Line ; and therefore if no Force makes the Pendulum fly out farther than ordinary in its Vibrations, they will be all perform'd in the same Time, because then the Cycloidal Arcs are describ'd.

Now, at Sea the Motion of the Ship will cause the Pendulum to make large, and sometimes small Vibrations : But if it be answer'd, That a Check may be put to confine the Pendulum to vibrate in the Arc D π ; I say, That as much as the Spring or Contrivance, which checks the Pendulum, is acted upon by the said Pendulum when it endeavours to fly out beyond its Bounds, so much Motion is there added to the returning Pendulum, (because the Action and Reaction are always equal and contrary) and therefore its Velocity is too much increased,

Etc.
This will always remain an uncorrectable ~~Perfection~~ ^{Irreparable} ~~against Pendulum-Clocks~~ ^{for the} Ship

Ship should not roll, (which never was known;) yet such a Clock would be useless: For, let us suppose the Ship to go very steady, upon the least increase of the Ship's Velocity, the Pendulum will swing fore or aft with too great a Force, as for Example to p. If the Ship's Velocity be diminish'd, the Pendulum swings from Side to Side, the rolling (which we now consider again) will by its Irregularity, produce the above-mention'd Effect; and this is all built upon this certain Principle, *viz.* That all moving Bodies, if acted upon by no extrinsical Agent, always continue in their State of Motion: So the Pendulum, which, together with the Ship, was going forward with a determinate Degree of Velocity, continues to go on with the same Velocity, even when that of the Ship is diminished, and so flies out too far, &c. And so likewise the contrary happens, if the Ship is accelerated, &c. the Pendulum either making too long, or too short Vibrations.

I take no Notice of the lengthening of the Pendulum-Rod by Heat, and its contracting by Cold, because that may be rectified by a Thermometer, and the Pendulum may be shorten'd, as you approach the Æquator by a Table of the different Lengths requir'd to swing Seconds in different Latitudes.

What I propose therefore, is, a Spring-Movement.

Methinks I hear Mr. H——'s answer, That I rob him of his Invention: But let us come to the Description of mine, and then let my Readers judge; but first take the several Steps that I made, before I came to a Certainty.

It is some Years since I thought the Matter feasible, conceiving that if I could by an exact Time-

keeper

keeper, find in any Part of the World, what a Clock it is at *Dover*, or any other Place assign'd, and at the same Time what a Clock it is where the Ship is, the Problem was solv'd; therefore I was resolv'd to spare no Pains and Cost to bring Clock-work to Perfection. When first the Pivots in Watches were made to go in Gems, I was resolv'd to try what that would do; but after having us'd Diamonds, I found that the Pivots would run in highly hammer'd Brass, almost as well; but upon second Consideration, I imagin'd that the Difficulty of polishing the Inside of the Hole in the Diamond, was the Cause that I had fail'd of Succes: Then I try'd Rubies, which I easily drill'd and polish'd, and then they succeeded beyond Expectation; for my Pivots being very hard, and very little Oil put in at first, I found the Oil was gone in a little Time, being as it were suck'd into the Stone; but the Movement went then as regular as before. One of my Watches was about five Inches Diameter, and instead of a Spring, I apply'd a long Pendulum, and it went four Years without differing above 3, 4, or 6 Seconds from the sydereal Time; but the great Difficulty was, how to make a Spring and Balance perform the same as a Weight and long Pendulum, which I thus found out, after having almost given over the Thoughts of it. I knew by Experiment, that the Pendulum-Rod was by almost $\frac{1}{10}$ of an Inch longer in the greatest Heat of Summer, than in the coldest Winter Weather, and therefore kept a Table of AEquation to correct the Error. This made me imagine, that the Irregularity of the Spring, (which I sometimes substituted, instead of the long Pendulum) was not so much owing to a Defect in the tempering of it, as to the Alterations made by different Degrees of Heat and Cold. Accordingly, taking a Spring made in

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the Manner represented in *Fig. 2.* and fixing it to the Board FGHE ; so that one End was fast to the Nail A, and the other loose with a Weight hanging at it as B, I found that upon the Scale behind it FH, the Weight descended in hot, and ascended in cold Weather ; so that Heat not only lengthen'd, but weaken'd my Spring, and Cold contrac'ted it, and added to its Elasticity. It was in *December* that I try'd my Experiment, and hanging my Board with a Thermometer by it in a Green-house, I made it, from the Coldness of the Weather, gradually to sustain Heat, which I increas'd 'till it became greater than the greatest in Summer, so as to reach and exceed that in any Latitude, and thereby had a new Thermometer made of the Spring. I try'd several Springs this Way, and made a Spring-Movement with Springs thus try'd, and also apply'd 'em to my above-mention'd Clock, (which has gone four Years without any Oil, that which was us'd at first seeming dry'd up) instead of Weights, and a Balance instead of the Pendulum, in such Manner, that all the Wheels stood vertical, that the Friction might be equal on the Pivots. I made this new Watch sustain all the Degrees of Heat and Cold, as it had before done when single, and made an *Æquation-Table*, by the Help of the Thermometer, as mention'd before, to correct the Time, always suffering the Machine to take its Course. I likewise try'd what Effect Moisture and Dryness had upon this Movement, by making a Steam in the Room, with a large Vessel like one of Mr. Savery's Boylers, and successively dropt cold and warm Water upon my Wheels, which I found to cause a considerable Irregularity on the Watch, tho' it did not seem to affect the Spring singly, unless according as the Vapour was hot or cold. I made no Table to settle the Matter of the

Moisture

Moisture and Dryness, because I keep my Machine in a Vacuum, and can wind it up without letting in the Air, as will appear in its Description. All that I am to do at Sea, is, to keep it as perpendicular as I can, that the Axes of the Wheels may be horizontal; but the Want of that now and then, can cause no great Error, especially since I suspend it like the Compass in concentrick Circles, and fix the whole to the Center of Gravity of the Ship.

The Way that I compar'd the going of my Watches with the true Time, was this: I made an Hole thro' a Wall about half an Inch Diameter, and upon the Gable End of an House, at some Distance, fix'd a strong Iron made in the Shape of DE, (Fig. 3.) so that looking thro' the hole in my Wall, and the Slit D in the Iron, I could see the *Bull's Eye* in the Slit; and when I could see the Bull's Eye again the next Night in the said Slit, I call'd that a sydereal Day, with which comparing my Machine as oft as the Darknes and Clearnes of the Night wou'd permit me, I found it not to vary above 6 Seconds. I must, by the by, take Notice, that I cou'd not by this Contrivance find any sensible Parallax of the fix'd Stars, whether I look'd with the naked Eye, when the Star seem'd to fill the whole Slit in the Iron, or with a small Telescope, when ceasing to twinkle it appear'd like a lucid Point in the Middle of the said Slit.

Here follows the Description of my Time-keeper. (See Fig. 4.)

HIKL is the Movement, with its vertical Dial-Plate, and its three Hands, viz. Hour-Hand, Minute-Hand, and Second-Hand, fix'd to the horizontal Brass Plate MN.

MXAECXM is a Glass Receiver from which the Air is drawn out at the Passage F, which has a Valve to apply an Air-Pump or Syringe to, and then a Brass Head

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Head to screwe over the Valve and more firmly binder the Return of the external Air; but yet so as it may be taken off to apply the Syringe at any Time, if any Air shou'd have insinuated itself into the Receiver; but to secure it, there is a wet Piece of Sheep's Leather on the Brass Plate, which is always kept moist by Means of Water that lies constantly on the Plate between the Receiver and the Brass Rim MN made high for that Purpose.

A is a Brass Collar full of oil'd Leathers, thro' which a Key passes, to wind up the Movement at G, in such manner, that no Air shall pass in whilst the Clock is winding up; and that the winding up may not stop the Movement, thro' the Collar C slips another Key, to give Liberty to a Spring at F, which keeps the Watch going, whilst the other Key winds it up.

XX is the Rim of the Brass Cap of the Receiver, which rises so high as to hold Water to keep moist the oil'd Leathers of the Screws of the Collars A and C, and of the Screw at E.

At M and N are two Ends of an Axis for the Movement, Receivers, and Plate to run freely in the strong Brass Hoop POQ, which likewise, by means of the Iron Point QT, and another (which is here suppos'd behind the Machine) moves in the other Brass Hoop RST) which last Hoop has four strong triangular Plates, three of which appear in the Figure) by means of which the whole Engine is to be screw'd fast at or near the Center of Gravity of the Ship.

V V W W is a Weight of Lead so fix'd to the Plate on which the Movement stands, as to keep the Watch always perpendicular, or at least to bring it back to a vertical Position, when it is shak'd out of it; for our Watch is not accelerated or retarded by the mere shake out of a perpendicular Position, but by lying so long in another Position, as to have one End of the

Axa

Axes of the Wheels suffer more Friction than the other.

By means of the Glass Receiver, the Watch is kept from being affected with the Moisture and Dryness of the Air.

And the Thermometer, which is always to be near the Movement, shews, by Help of my Table, when the Work goes too fast, or too slow, and how much too fast, or how much too slow.

As for my Method of knowing what a-Clock it is at the Place where the Ship is, I shan't trouble my Reader with it, 'till I come back and mention it in the Memorial which I shall present to the Commissioners, and prove by Witnesses; for that is a Postulatum to a *Longitudinarian*, and I don't know one of 'em who makes any Difficulty of it.

Now, gentle *Mechanico-Mathematical* Reader, I humbly submit to thee, and leave thee to judge, whether or not my Method will do for finding the *Longitude at Sea*, and whether all those that have been hitherto publish'd do not much fall short of mine.—

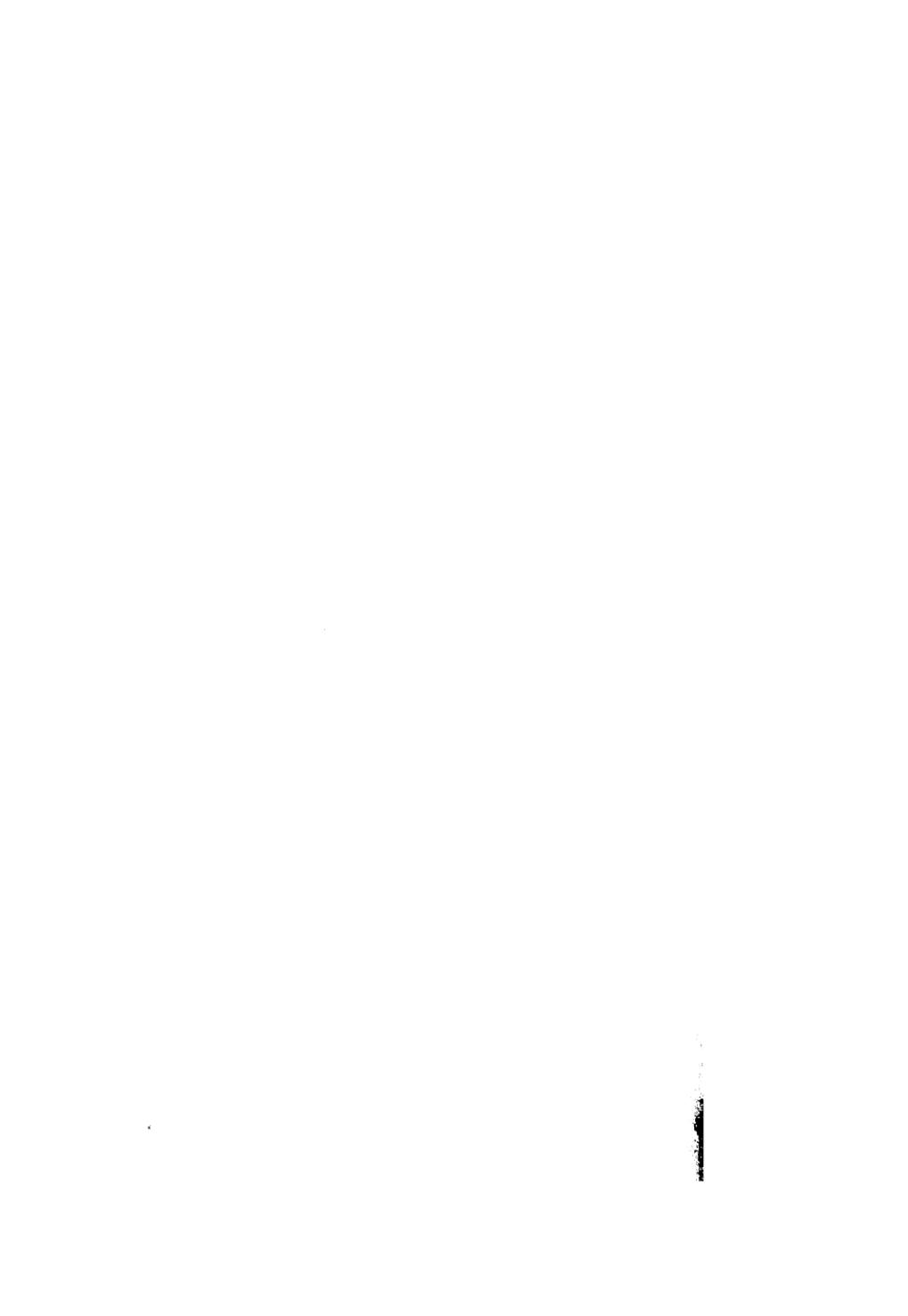
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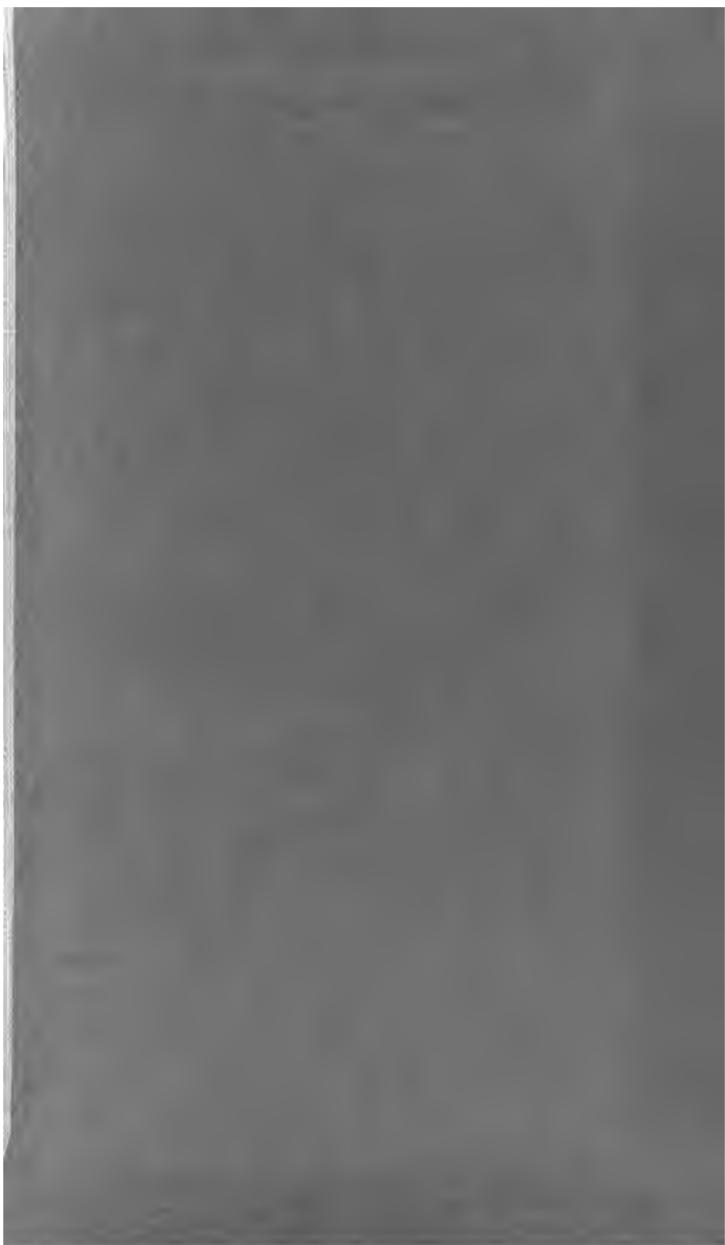
Jamq; Opus exegi—

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